



40 Zettabyte

Big Data Era

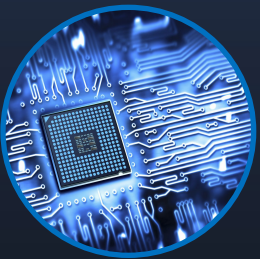
# The big problem: Scalability



Visualization



Algorithm



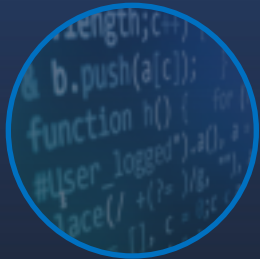
Hardware



# The big problem: Scalability



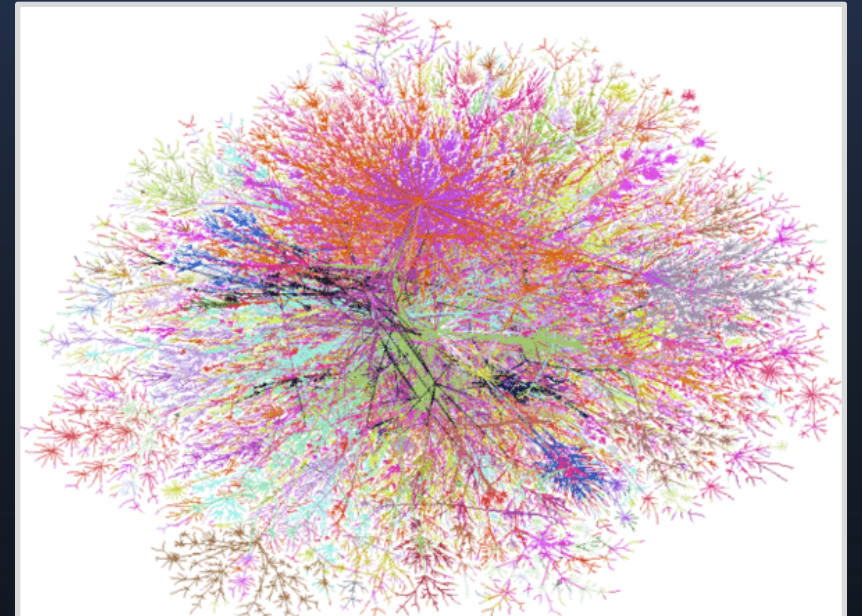
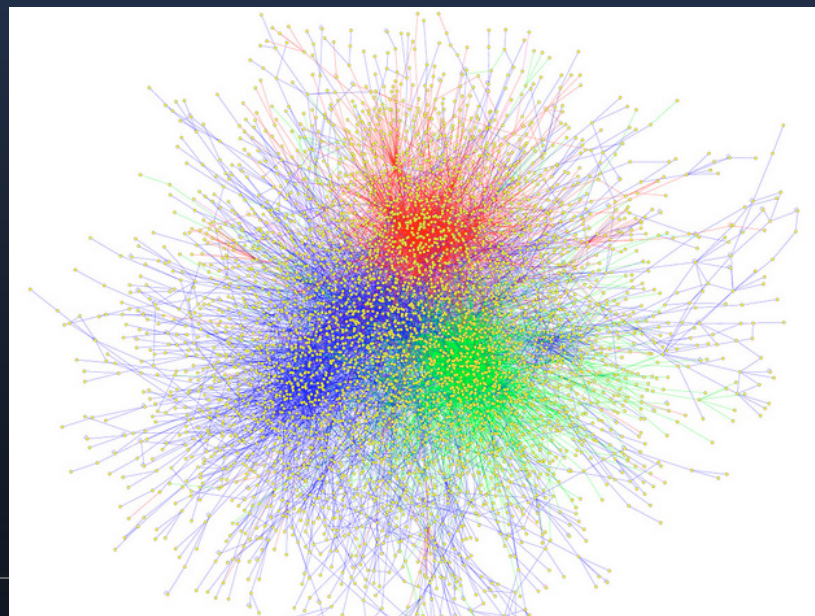
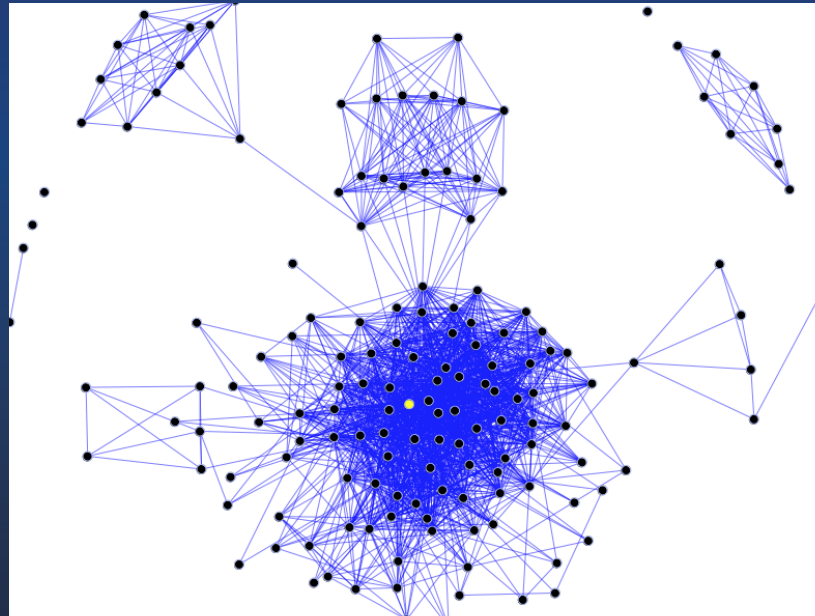
Visualization



Algorithm

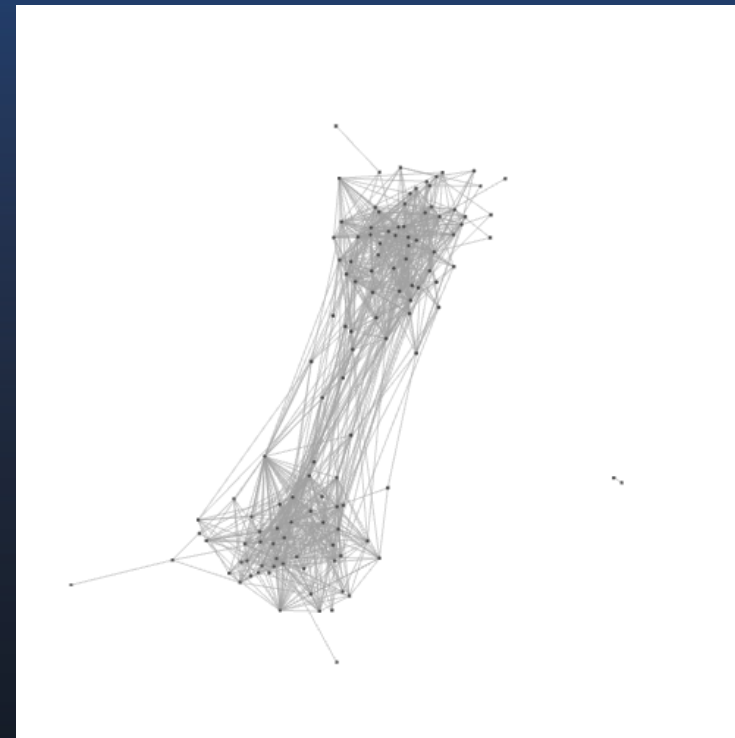
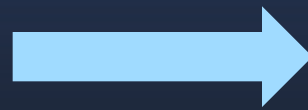
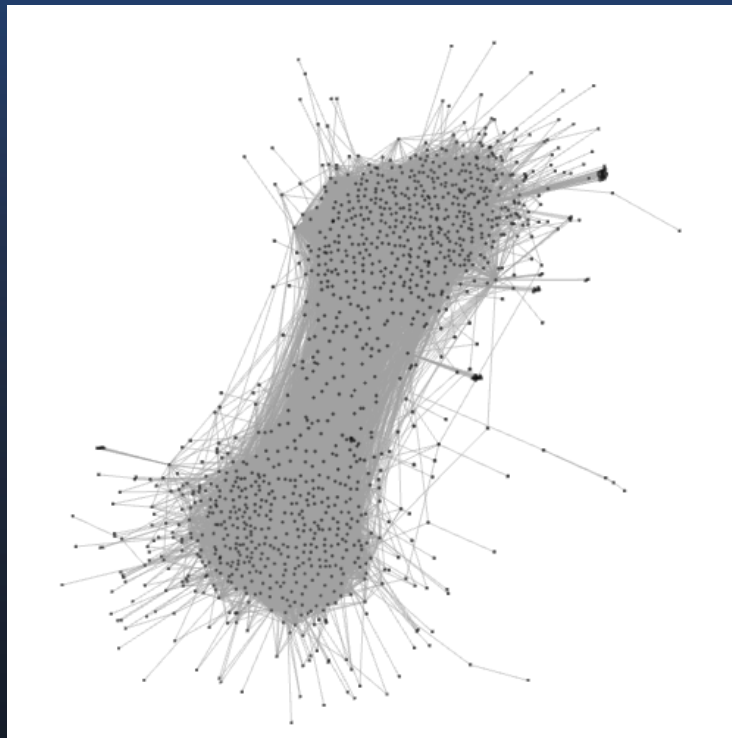


Hardware



# Graph Sampling

- Randomly pick nodes /edges to construct a **subgraph** that represents the original unfiltered graph:







Which sampling strategy to use?

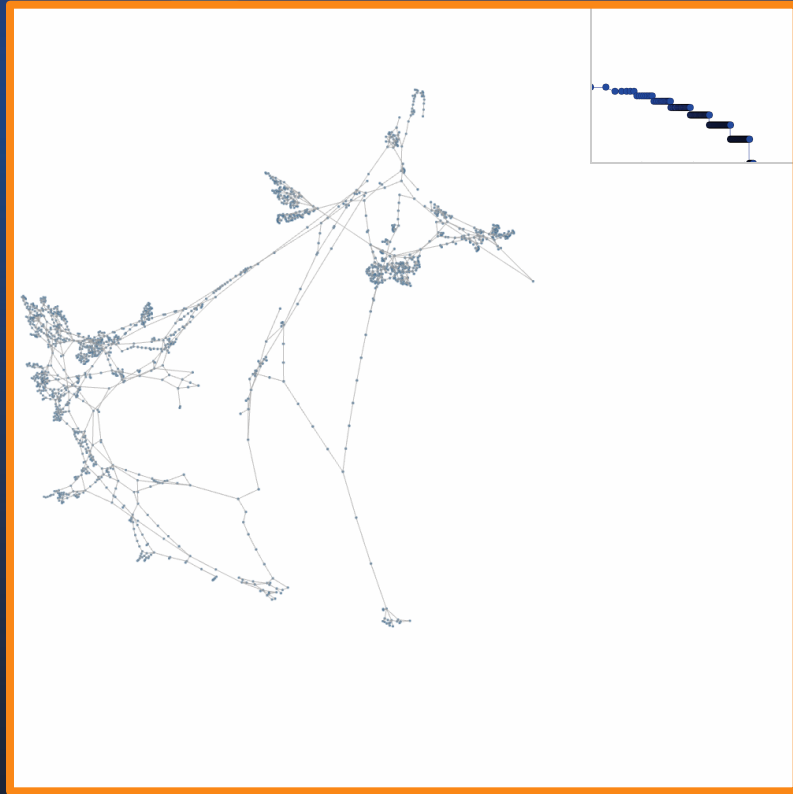
# Graph Sampling Evaluation

	Static graph patterns								Temporal graph patterns				AVG
	in-deg	out-deg	wcc	scc	hops	sng-val	sng-vec	clust	diam	cc-sz	sng-val	clust	
RN	0.084	0.145	0.814	0.193	0.231	0.079	0.112	0.327	0.074	0.570	0.263	0.371	0.272
RPN	<b>0.062</b>	<b>0.097</b>	0.792	0.194	<b>0.200</b>	0.048	0.081	0.243	0.051	0.475	0.162	0.249	0.221
RDN	0.110	0.128	0.818	0.193	0.238	0.041	0.048	0.256	0.052	0.440	<b>0.097</b>	0.242	0.222
RE	0.216	0.305	<b>0.367</b>	0.206	0.509	0.169	0.192	0.525	0.164	0.659	0.355	0.729	0.366
RNE	0.277	0.404	0.390	0.224	0.702	0.255	0.273	0.709	0.370	0.771	0.215	0.733	0.444
HYB	0.273	0.394	0.386	0.224	0.683	0.240	0.251	0.670	0.331	0.748	0.256	0.765	0.435
RNN	0.179	0.014	0.581	0.206	0.252	0.060	0.255	0.398	0.058	0.463	0.200	0.433	0.258
RJ	0.132	0.151	0.771	0.215	0.264	0.076	0.143	<b>0.235</b>	0.122	0.492	0.161	<b>0.214</b>	0.248
<b>RW</b>	0.082	0.131	0.685	0.194	0.243	0.049	<b>0.033</b>	<b>0.243</b>	<b>0.036</b>	<b>0.423</b>	<b>0.086</b>	0.224	<b>0.202</b>
<b>FF</b>	0.082	0.105	0.664	0.194	<b>0.203</b>	<b>0.038</b>	0.092	<b>0.244</b>	0.053	0.434	0.140	<b>0.211</b>	<b>0.205</b>

Random Walk (RW) v.s. Forest Fire (FF)

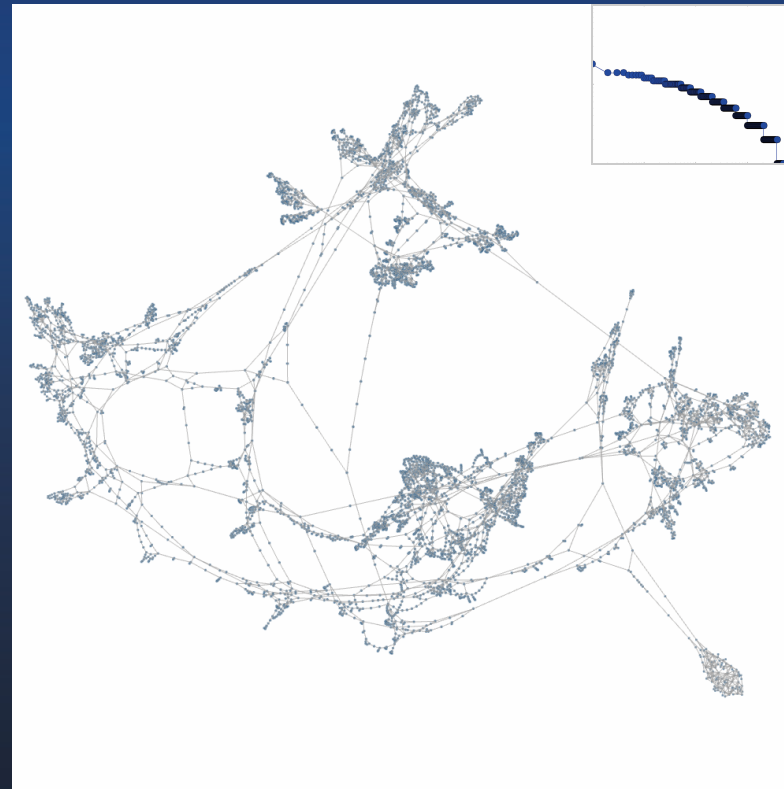
[Leskovec and Faloutsos, KDD 2006]

# Graph Sampling Evaluation in Visualization



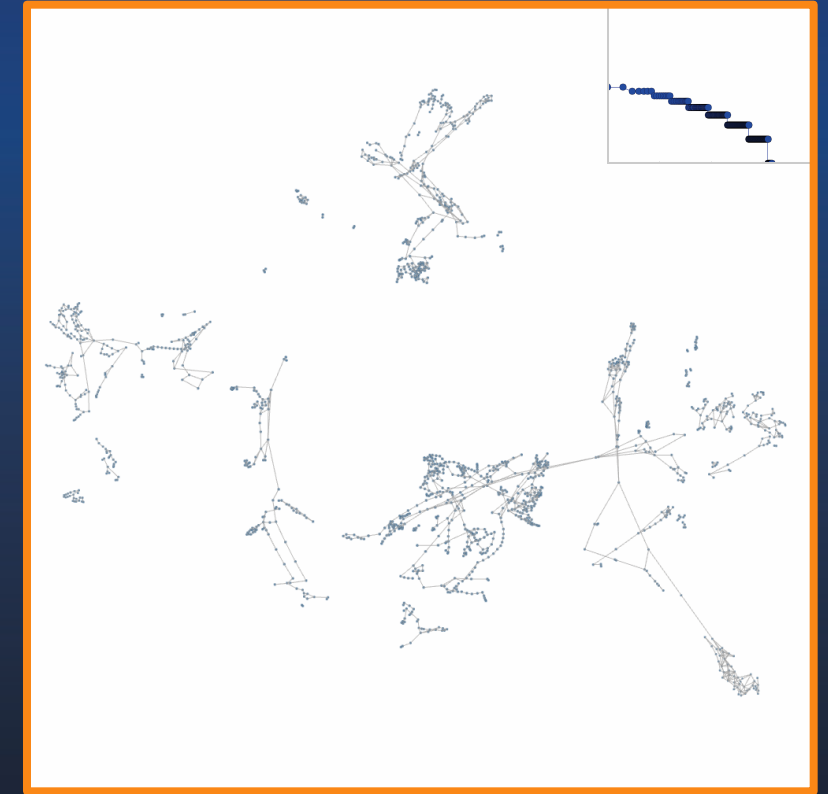
Random Walk (RW)

Avg. node degree: 2.4  
Power-law degree distribution



Original Graph

**Distinct Visual Result!**



Forest Fire (FF)

Avg. node degree: 2.4  
Power-law degree distribution



# Graph Sampling Evaluation in Visualization

## Similarity Measurements

Statistical  
Features:

Hub Inclusion  
Clustering Coeff.  
Discovery  
Quotient  
...

?

Data Mining

Visualization

# Graph Sampling Evaluation in Visualization

## Similarity Measurements

Statistical  
Features:

Hub Inclusion  
Clustering Coeff.  
Discovery  
Quotient  
...

Data Mining

Visual Factors:

?

Visualization

## Goals

G1: Identify the key **visual factors**  
that makes the sampled graphs **representative**

G2: Evaluate the **performance** of different  
sampling algorithms on these **visual factors**

## Procedure

Pilot  
Study

Formal  
Studies

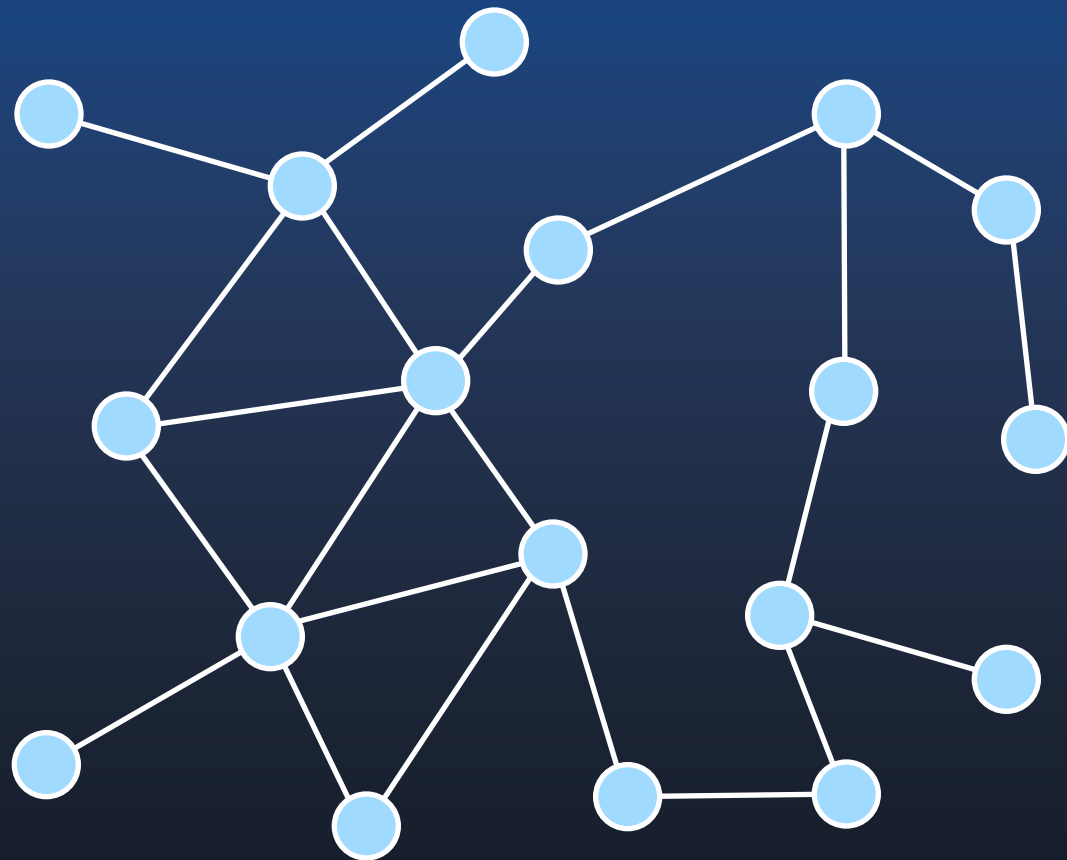


# Outline

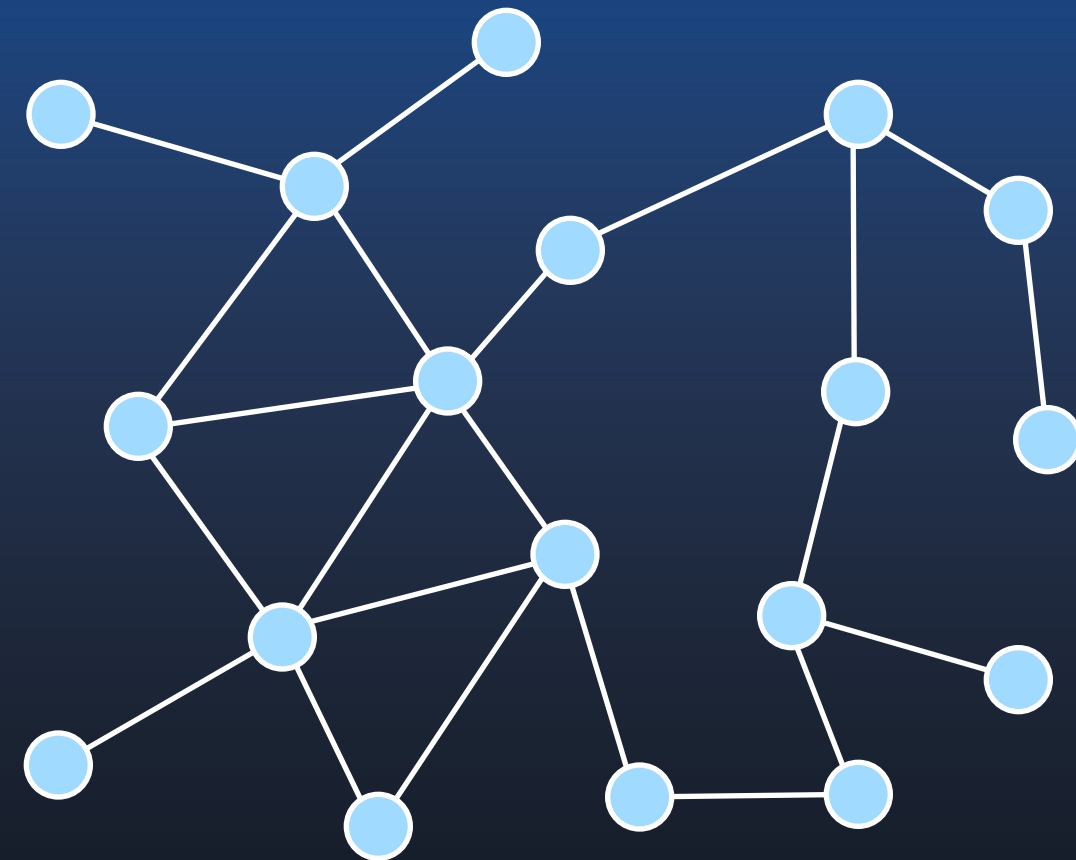
- Selected Sampling Methods
- Pilot Study
- Formal Studies
  - Perception of High Degree Nodes
  - Perception of Cluster Quality
  - Perception of Coverage Area



# Node-Based Sampling



Original Graph

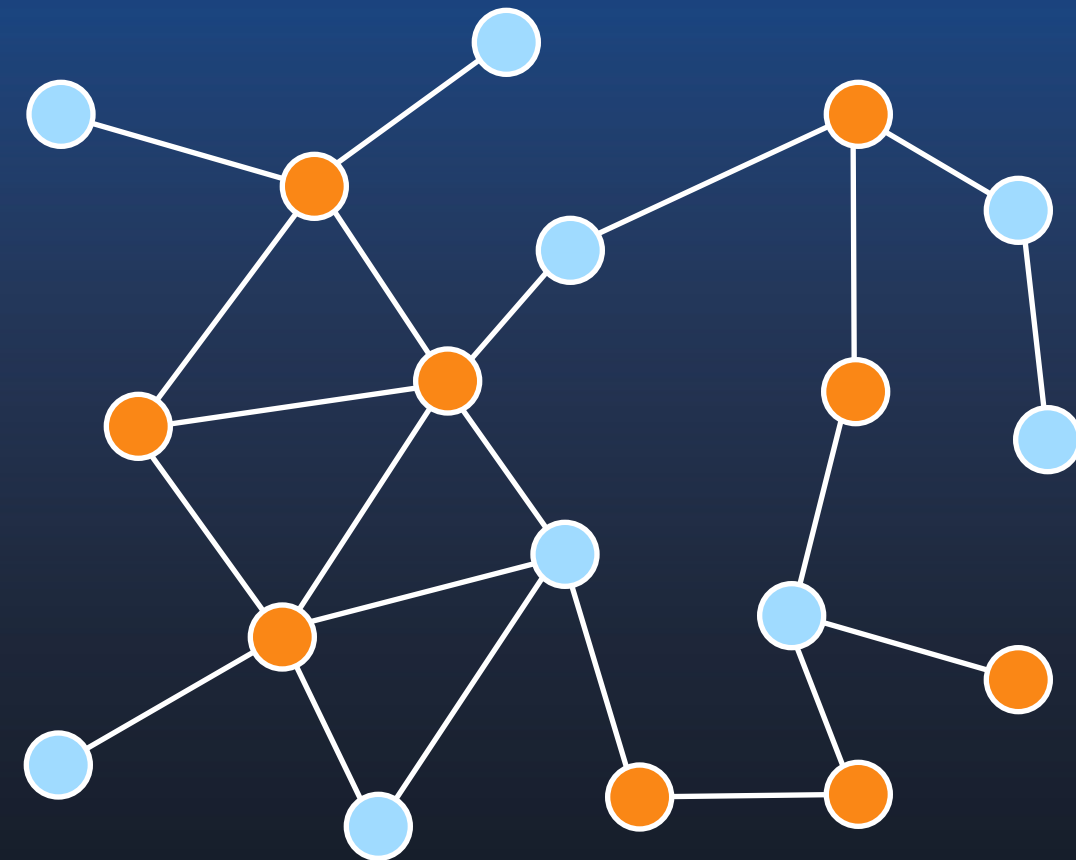


Random Node Sampling

# Node-Based Sampling

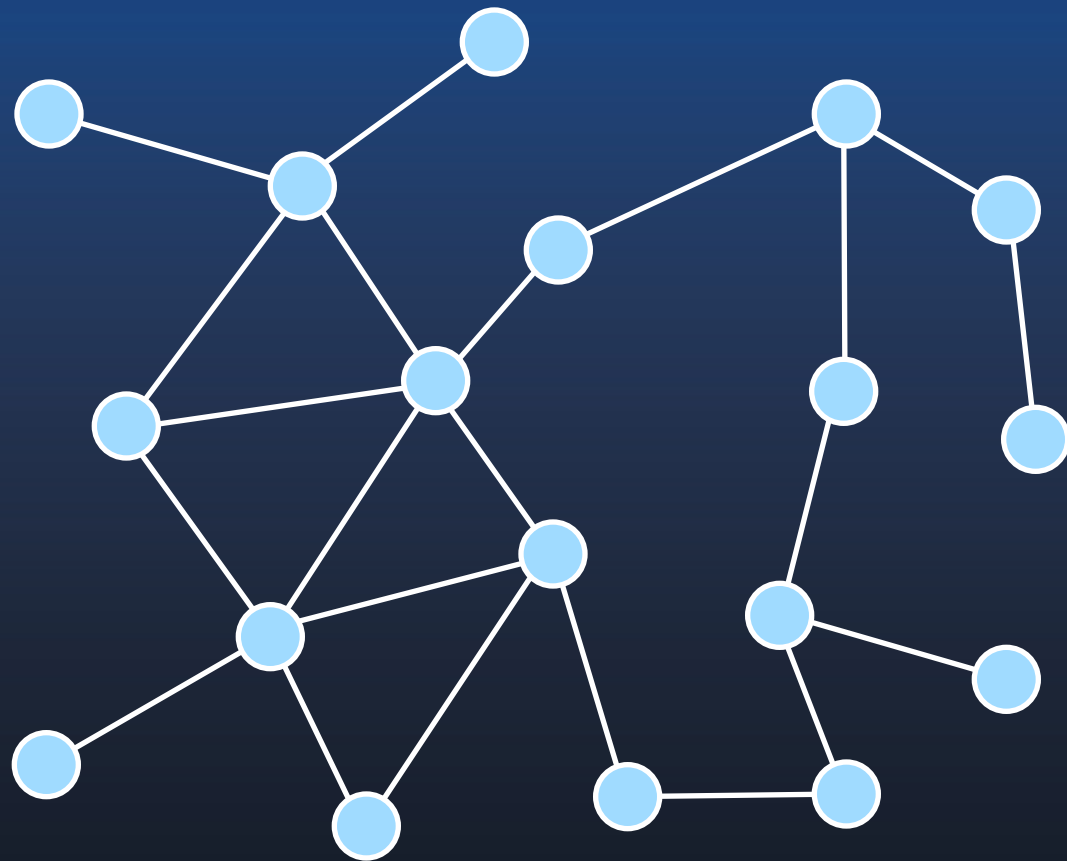


Original Graph

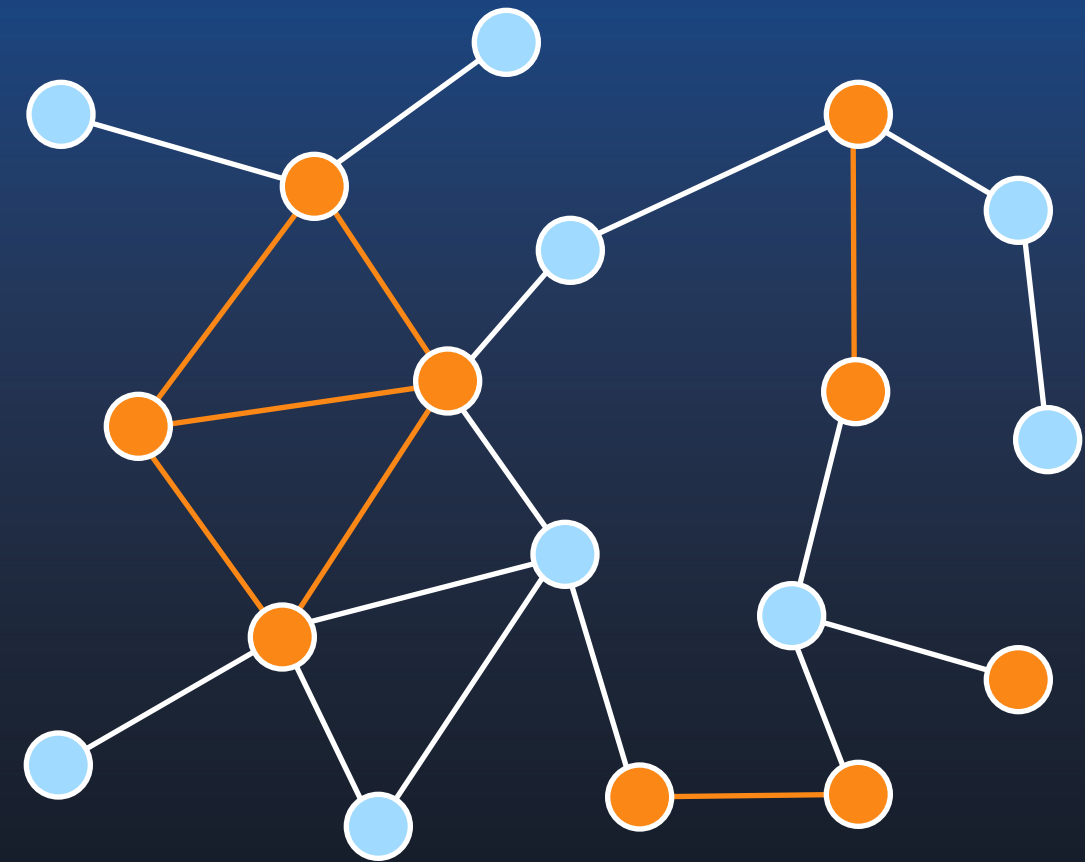


Random Node Sampling

# Node-Based Sampling



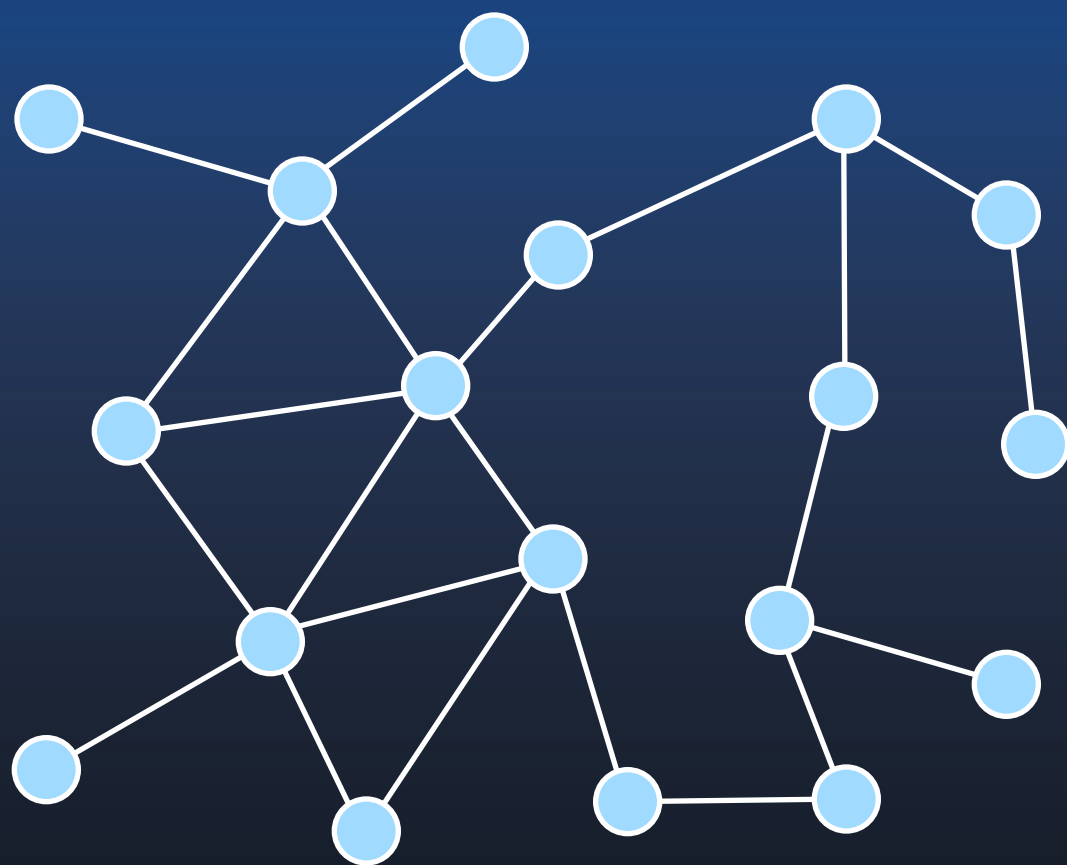
Original Graph



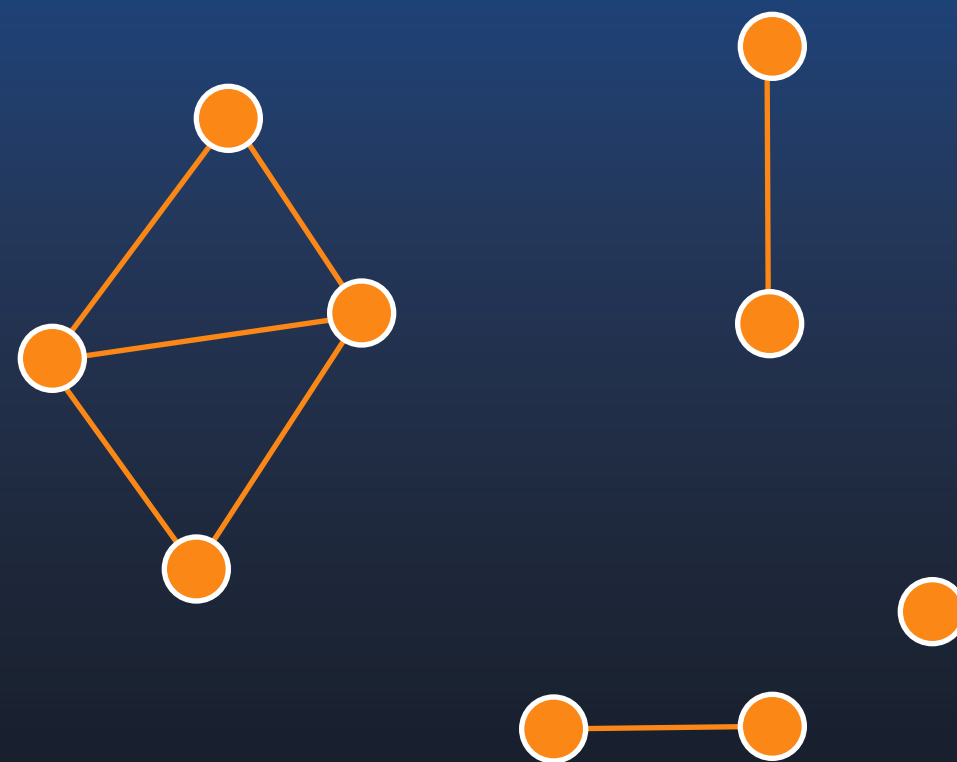
Random Node Sampling



# Node-Based Sampling

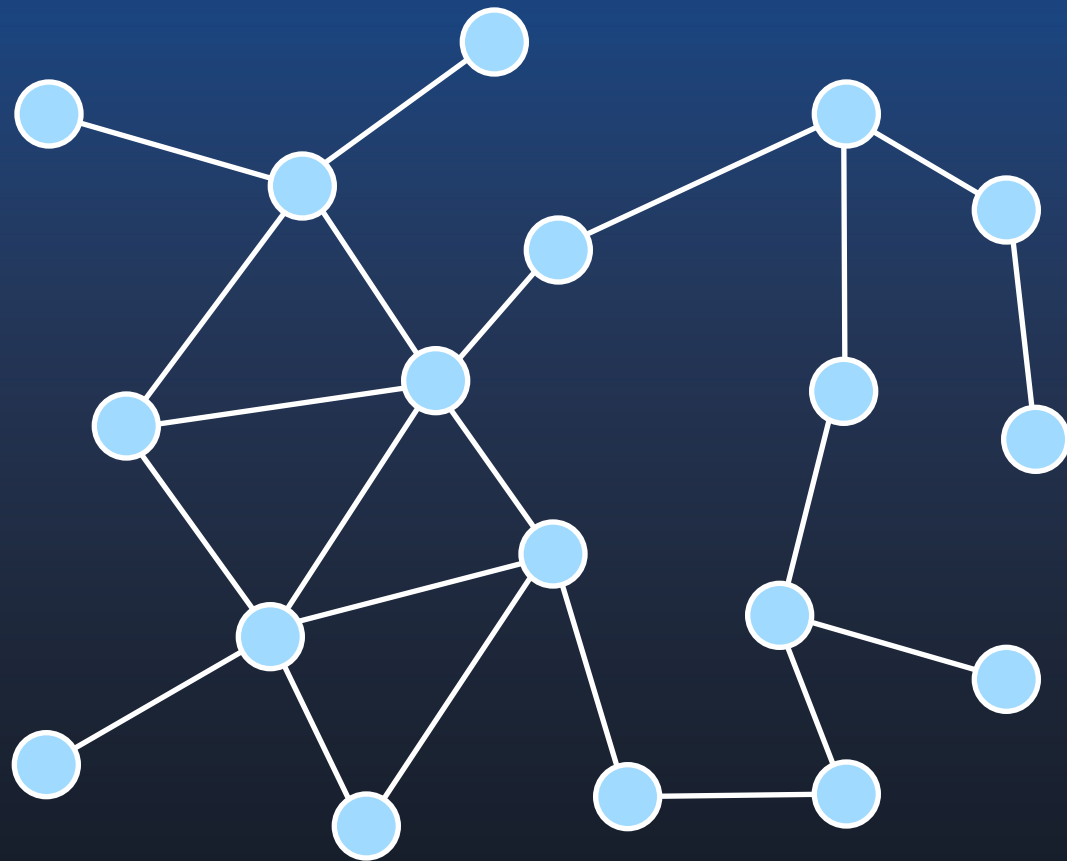


Original Graph

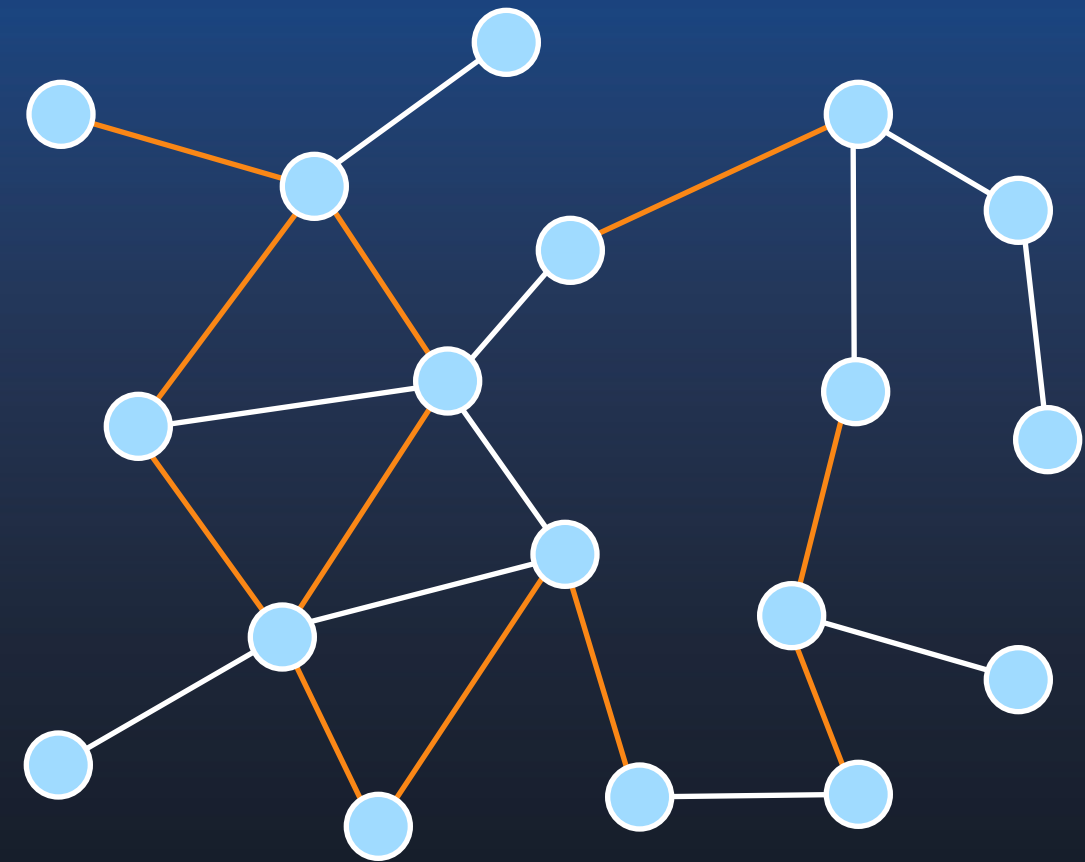


Random Node Sampling

# Edge-Based Sampling

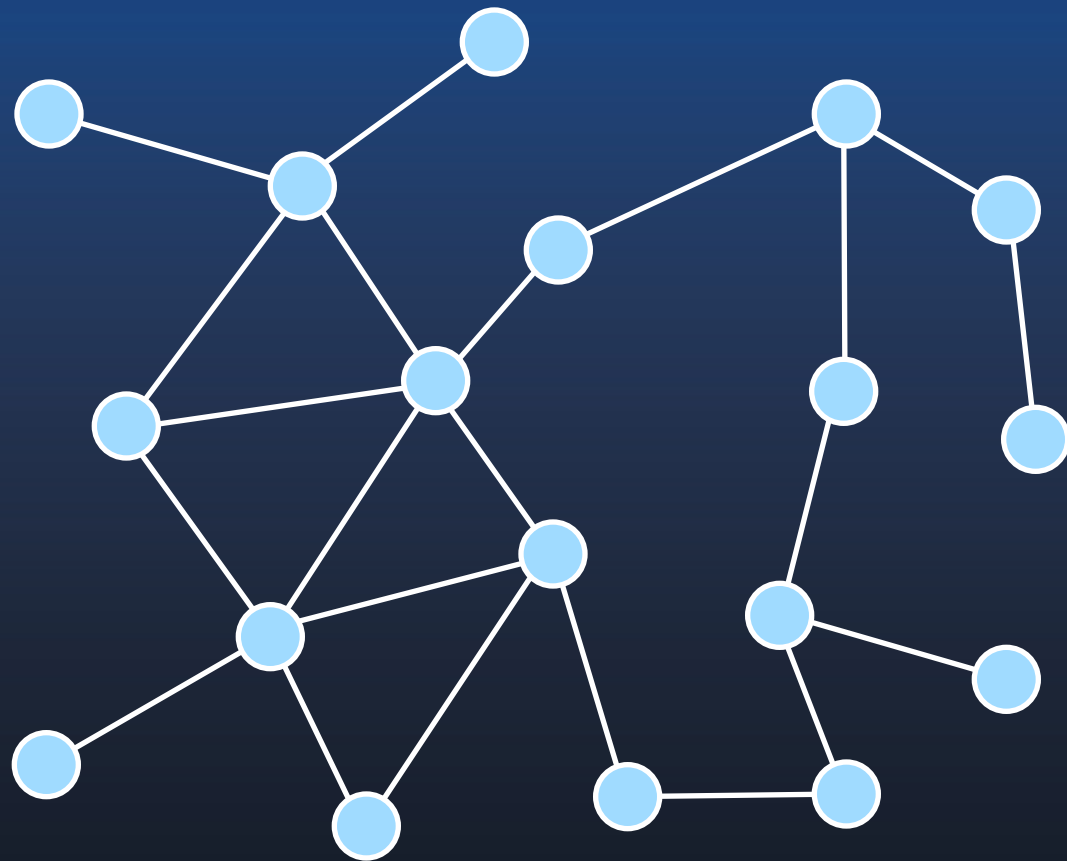


Original Graph

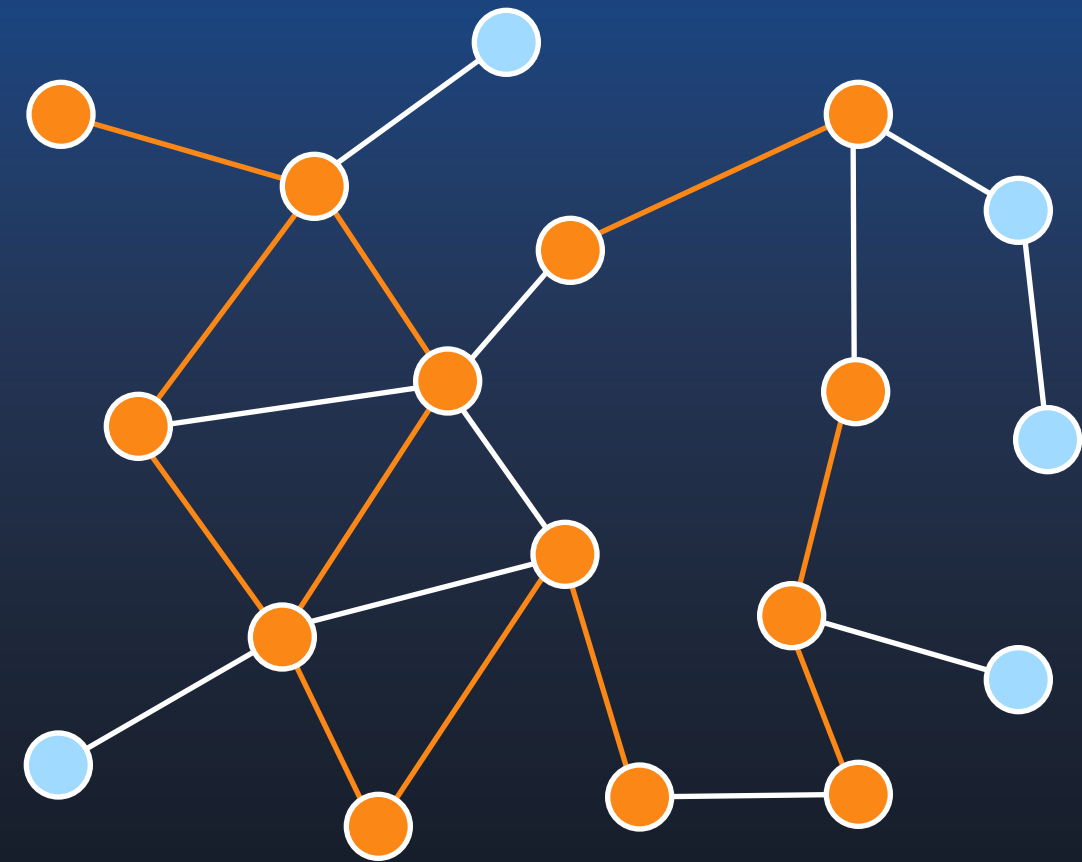


Random Edge Sampling

# Edge-Based Sampling



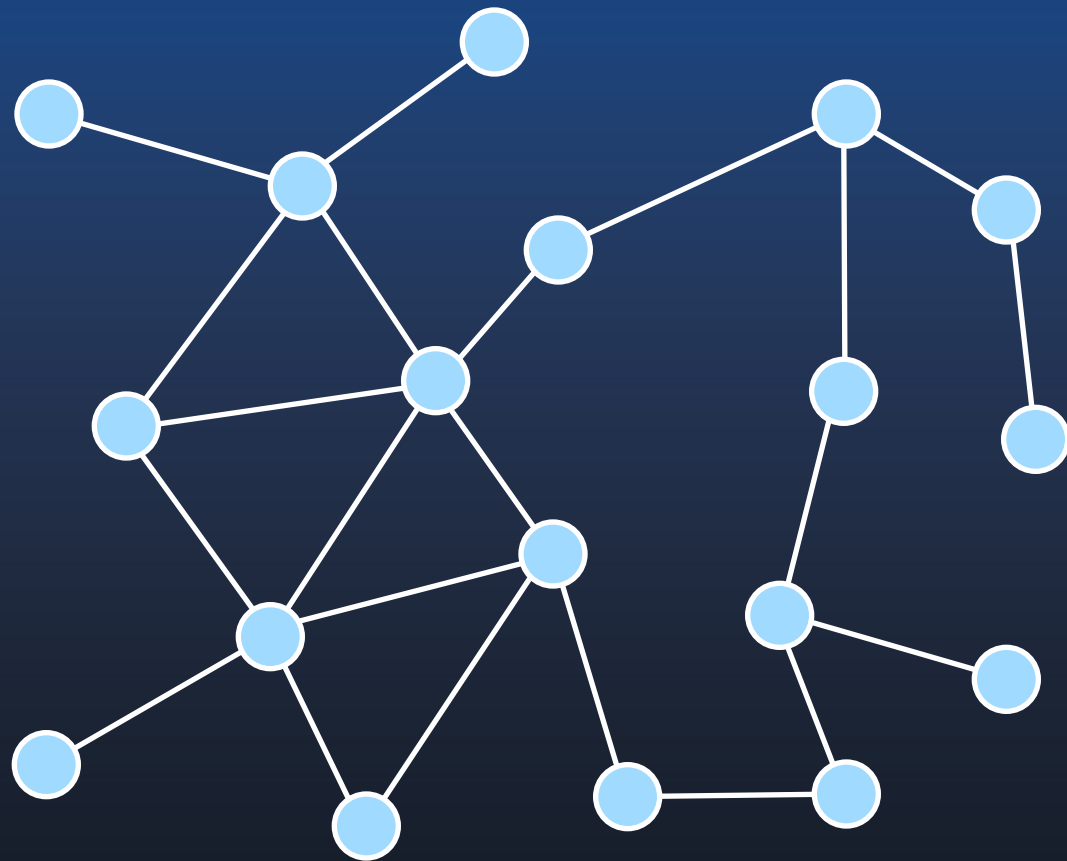
Original Graph



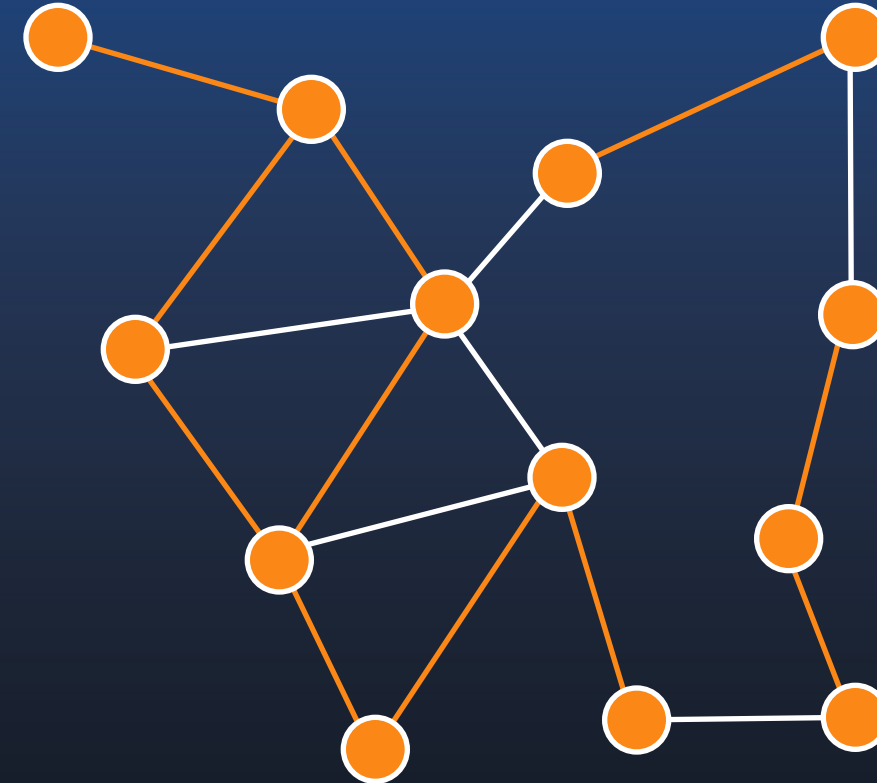
Random Edge Sampling



# Edge-Based Sampling

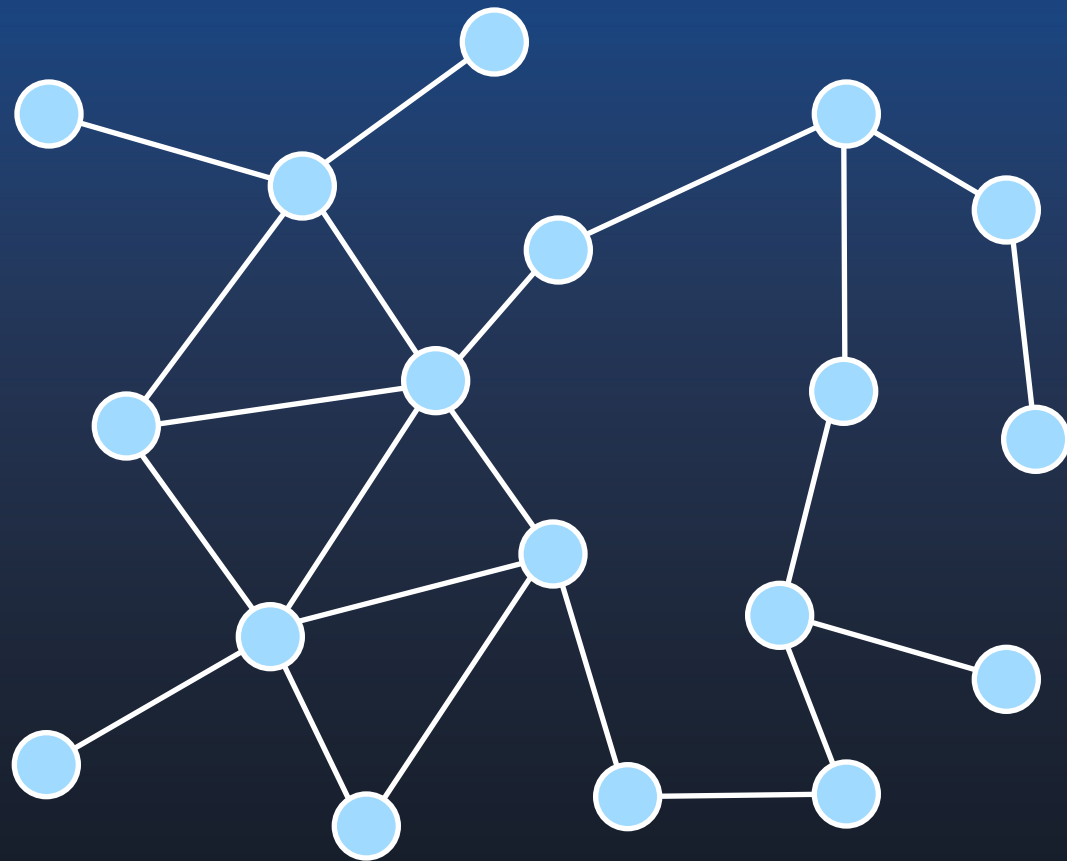


Original Graph



Random Edge Sampling

# Traversal-Based Sampling: Random Walk

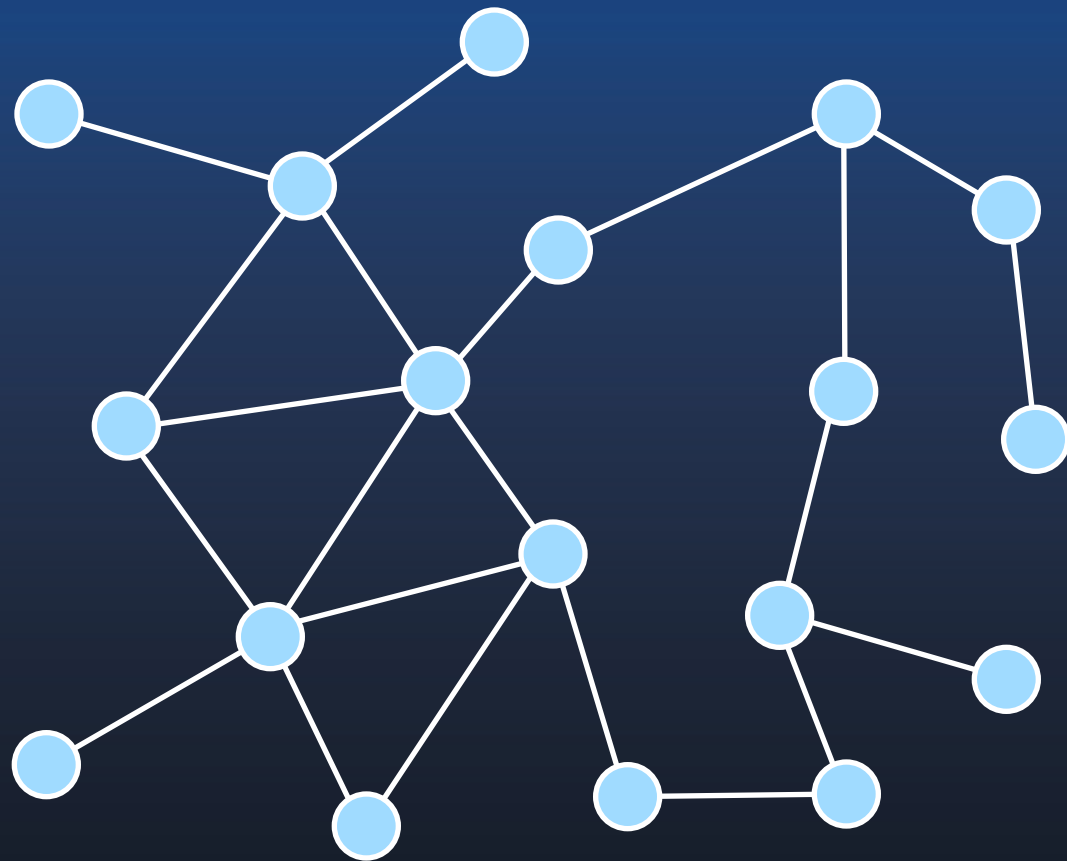


Original Graph

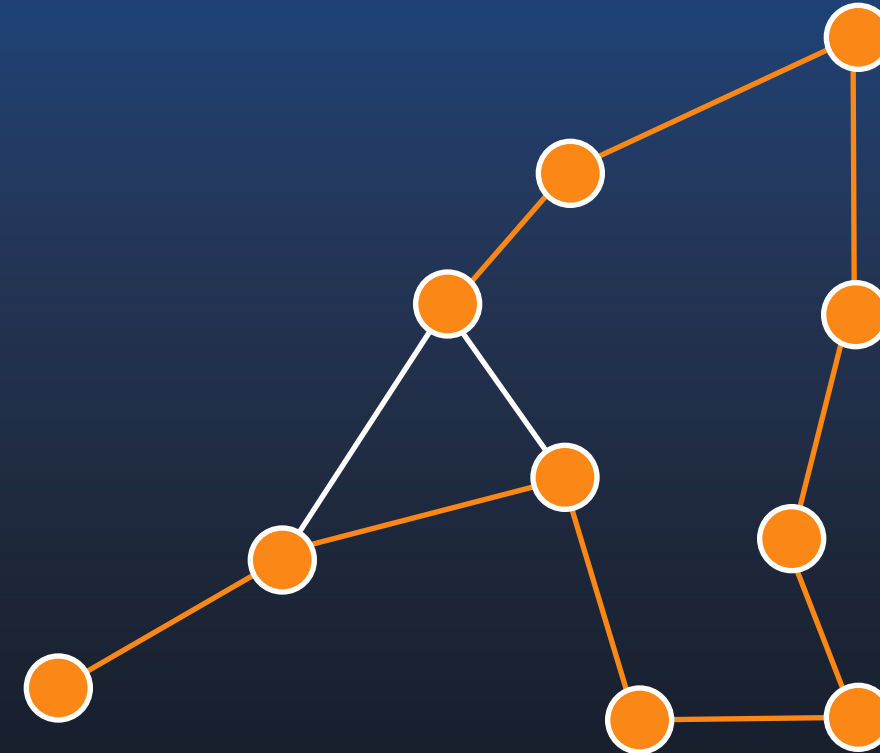


Random Walk

# Travel

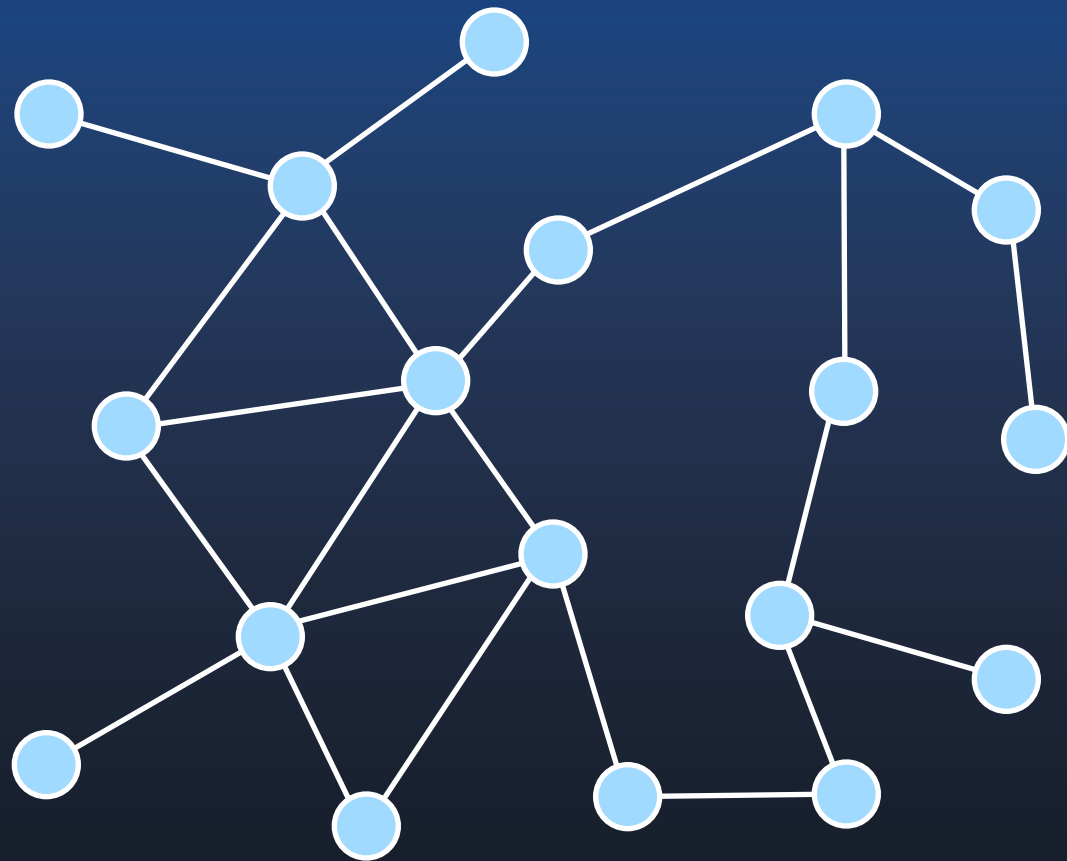


# Original Graph

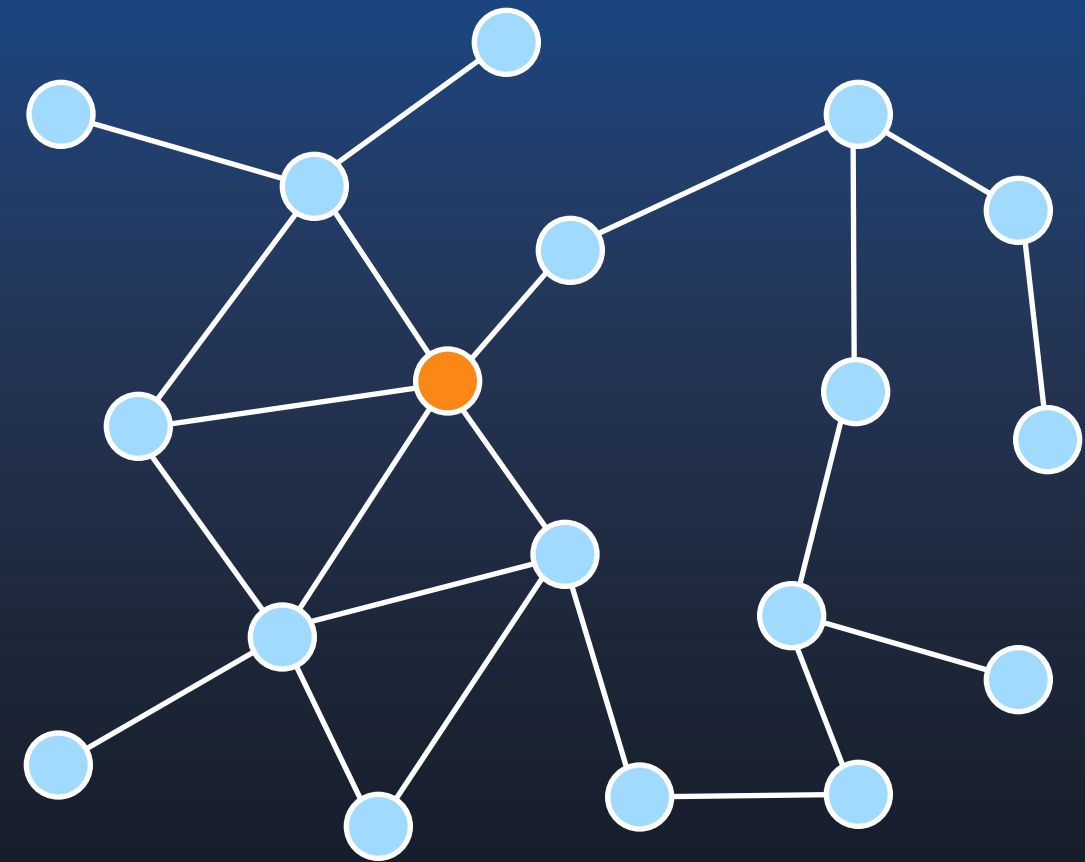


# Random Walk

# Traversal-Based Sampling: Random Jump



Original Graph

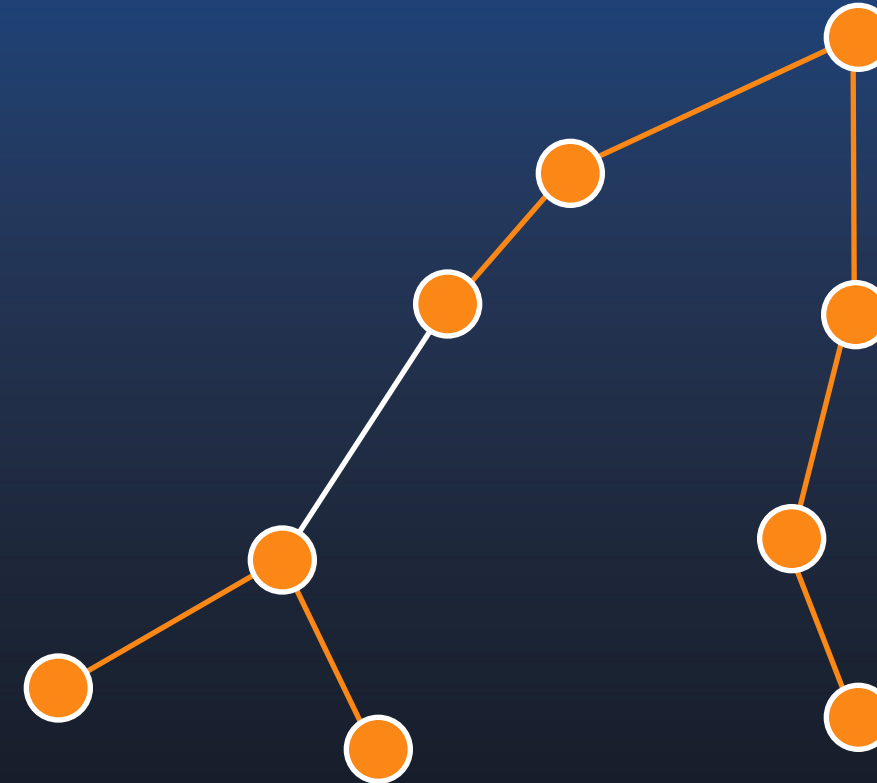


Random Jump

# Traversal-Based Sampling: Random Jump



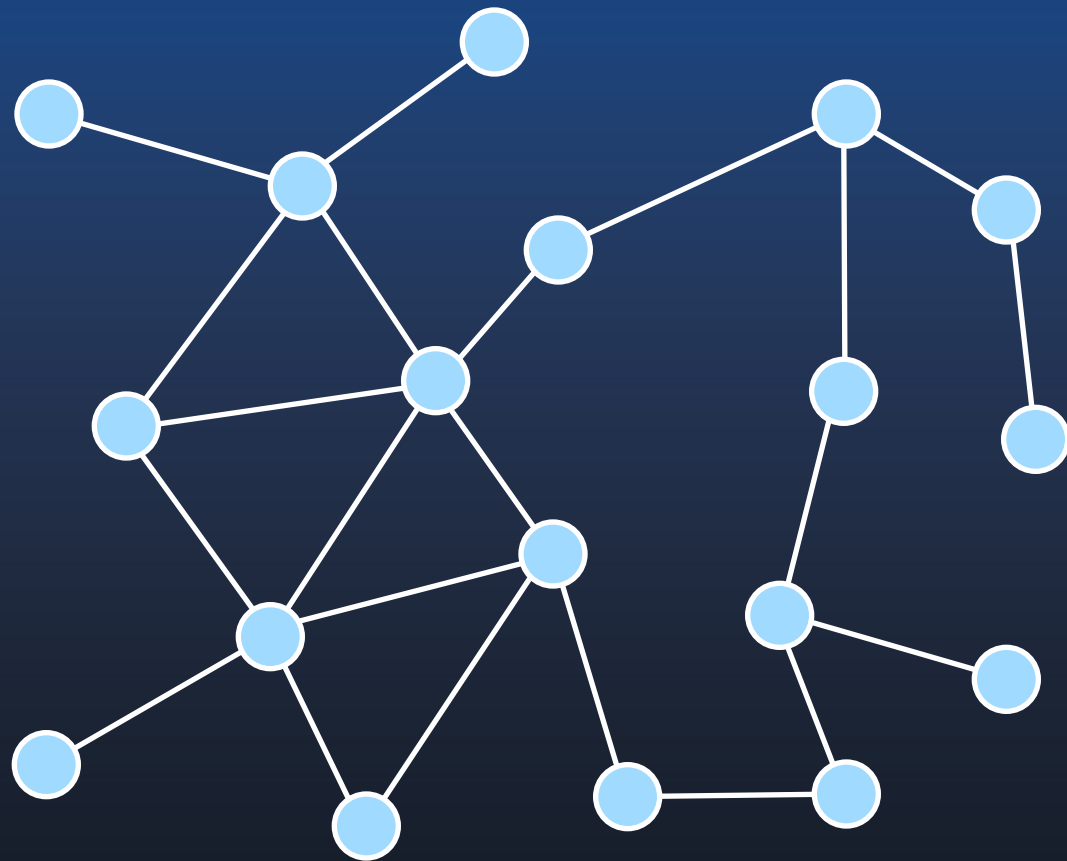
Original Graph



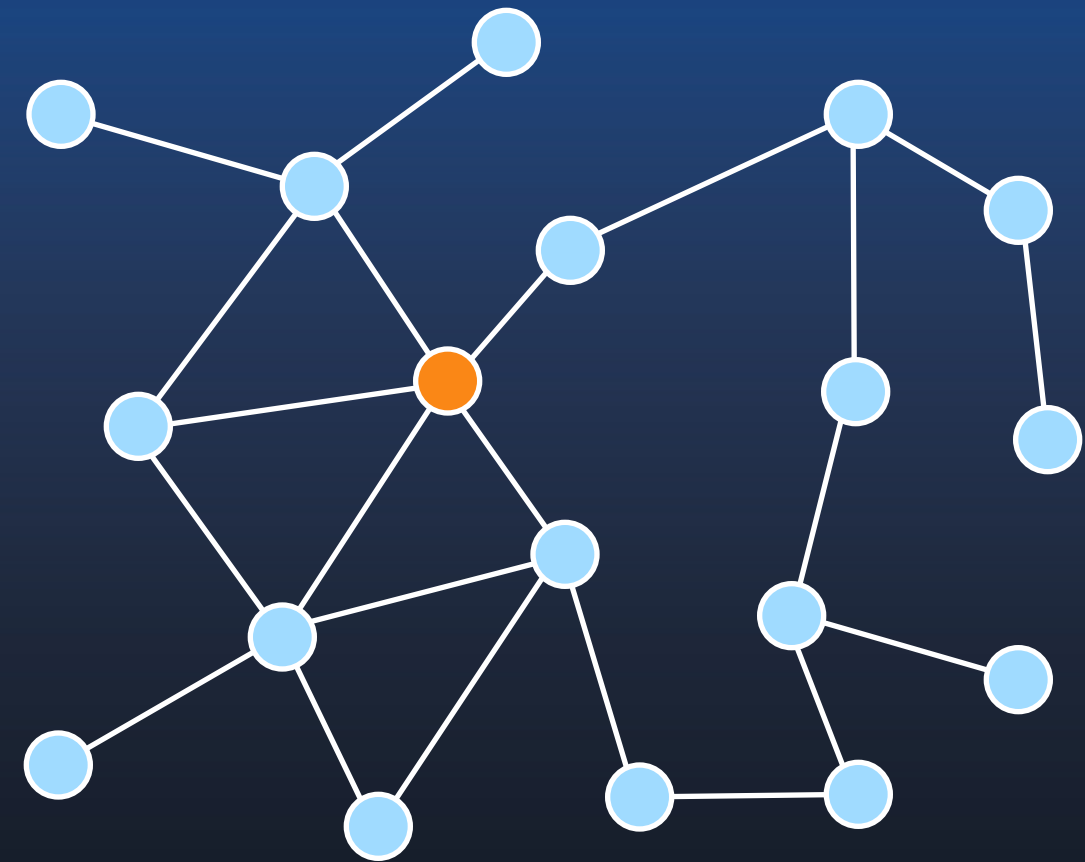
Random Jump



# Traversal-Based Sampling: Forest Fire

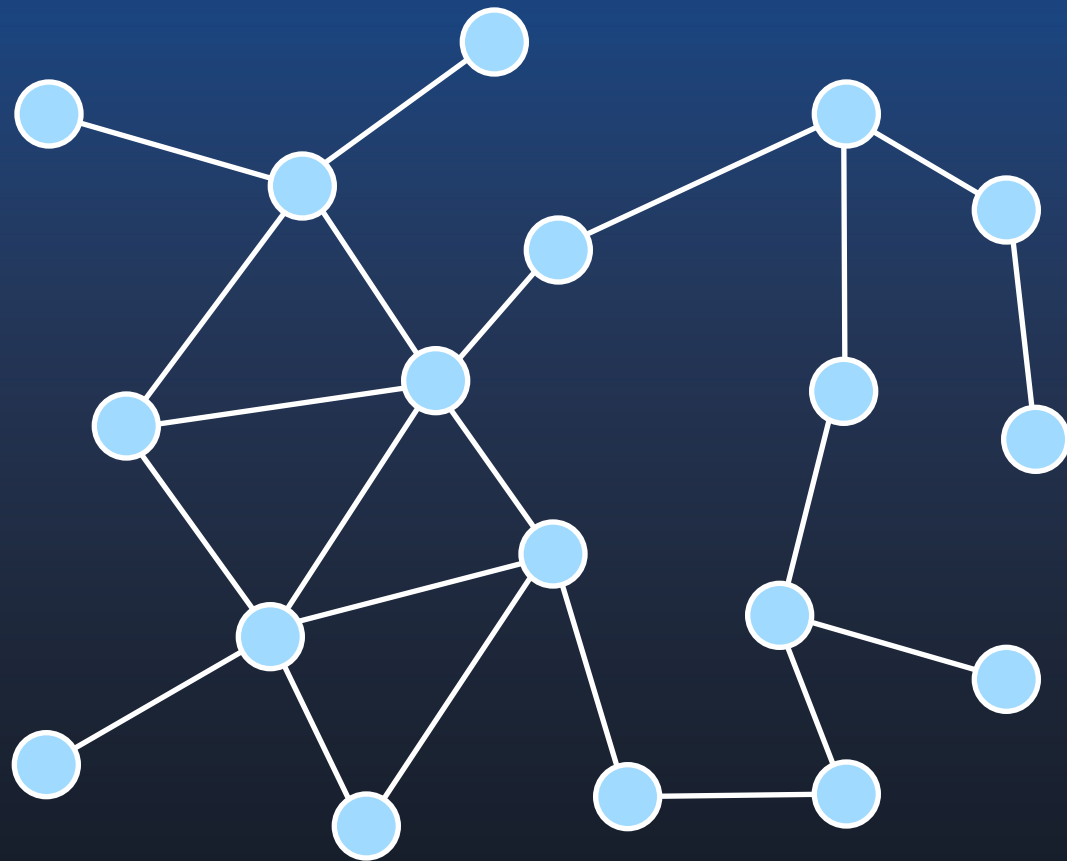


Original Graph



Forest Fire

# Traversal-Based Sampling: Forest Fire



Original Graph



Forest Fire



# Outline

- Selected Sampling Methods
- Pilot Study
- Formal Studies
  - Perception of High Degree Nodes
  - Perception of Cluster Quality
  - Perception of Coverage Area

# Pilot Study

- Task:
  - Identify the **visual factors** that strongly influence the representativeness of sampled graphs
  - We also determine the sampling rate used in the formal studies.

Network	N	D	AD	CC	PL
ResidentRating ( <i>RR</i> )	217	0.1002	21.6	0.50	1.9
PoliticalBlogs ( <i>PB</i> )	1,222	0.0220	27.4	0.32	2.7
AdolescentHealth ( <i>AH</i> )	2,539	0.0054	13.7	0.33	2.3
PowerGrid ( <i>PG</i> )	4,941	0.0005	1.3	0.08	19.0
Google+ ( <i>G+</i> )	23,613	0.0001	3.3	0.17	4.0

Dataset: 5 Real-World Graphs

Network Level	Node Level	Edge Level
Coverage Area ( <i>CA</i> )	High Degree Nodes ( <i>HN</i> )	Edges Linking <i>HN</i>
Cluster Quality ( <i>CQ</i> )	Margin Nodes ( <i>MN</i> )	Edges Linking <i>MN</i>
	Boundary Nodes ( <i>BN</i> )	Edges Linking <i>BN</i>

Visual Factor Candidates

# Pilot Study

- Task:
  - Identify the **visual factors** that strongly influence the representativeness of sampled graphs
  - We also determine the sampling rate used in the formal studies.

High Degree Nodes  
Cluster Quality  
Coverage Area

Results (key visual factors)

Network Level	Node Level	Edge Level
Coverage Area ( <i>CA</i> )	High Degree Nodes ( <i>HN</i> )	Edges Linking <i>HN</i>
Cluster Quality ( <i>CQ</i> )	Margin Nodes ( <i>MN</i> )	Edges Linking <i>MN</i>
	Boundary Nodes ( <i>BN</i> )	Edges Linking <i>BN</i>

Visual Factor Candidates

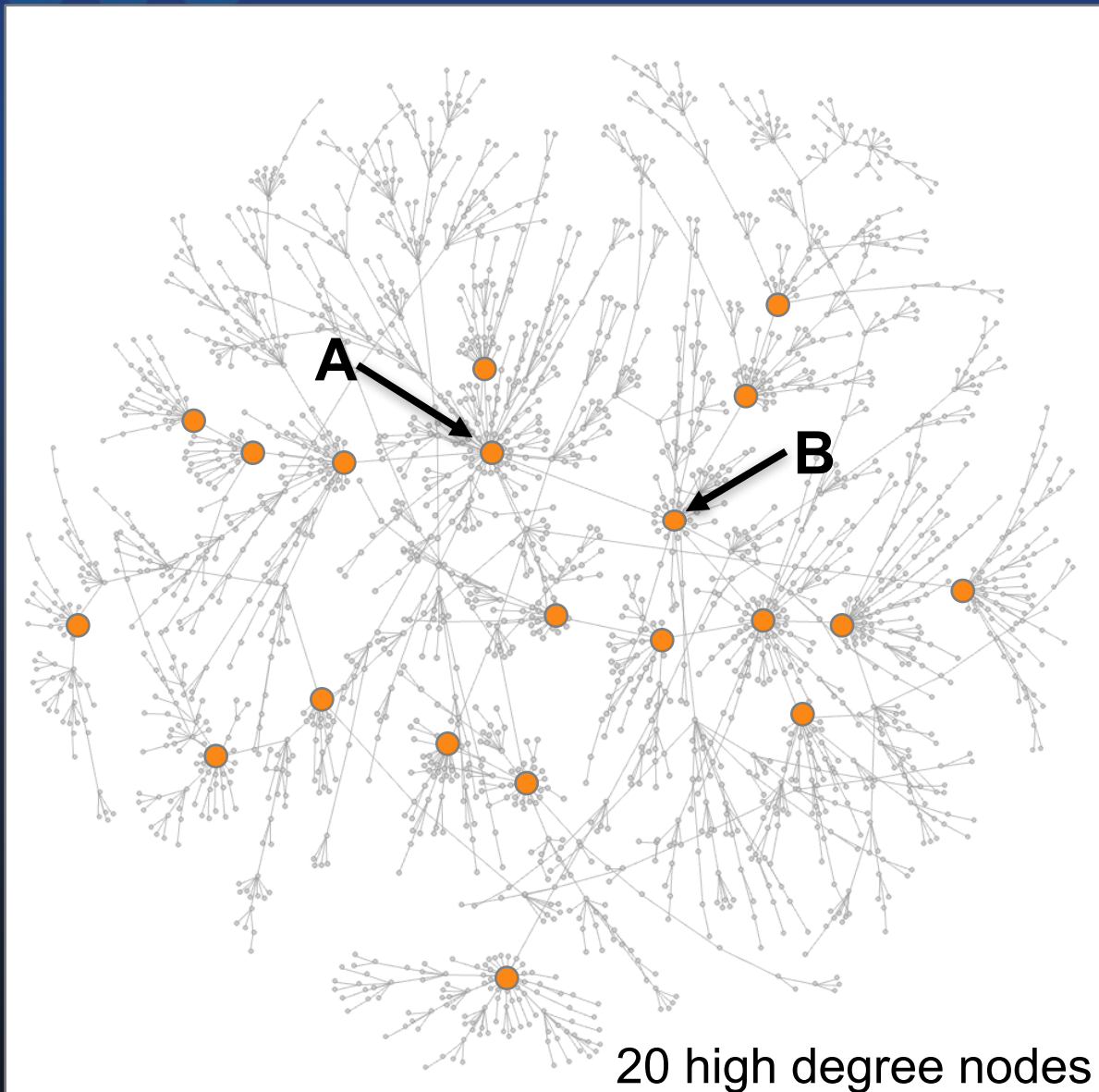


# Outline

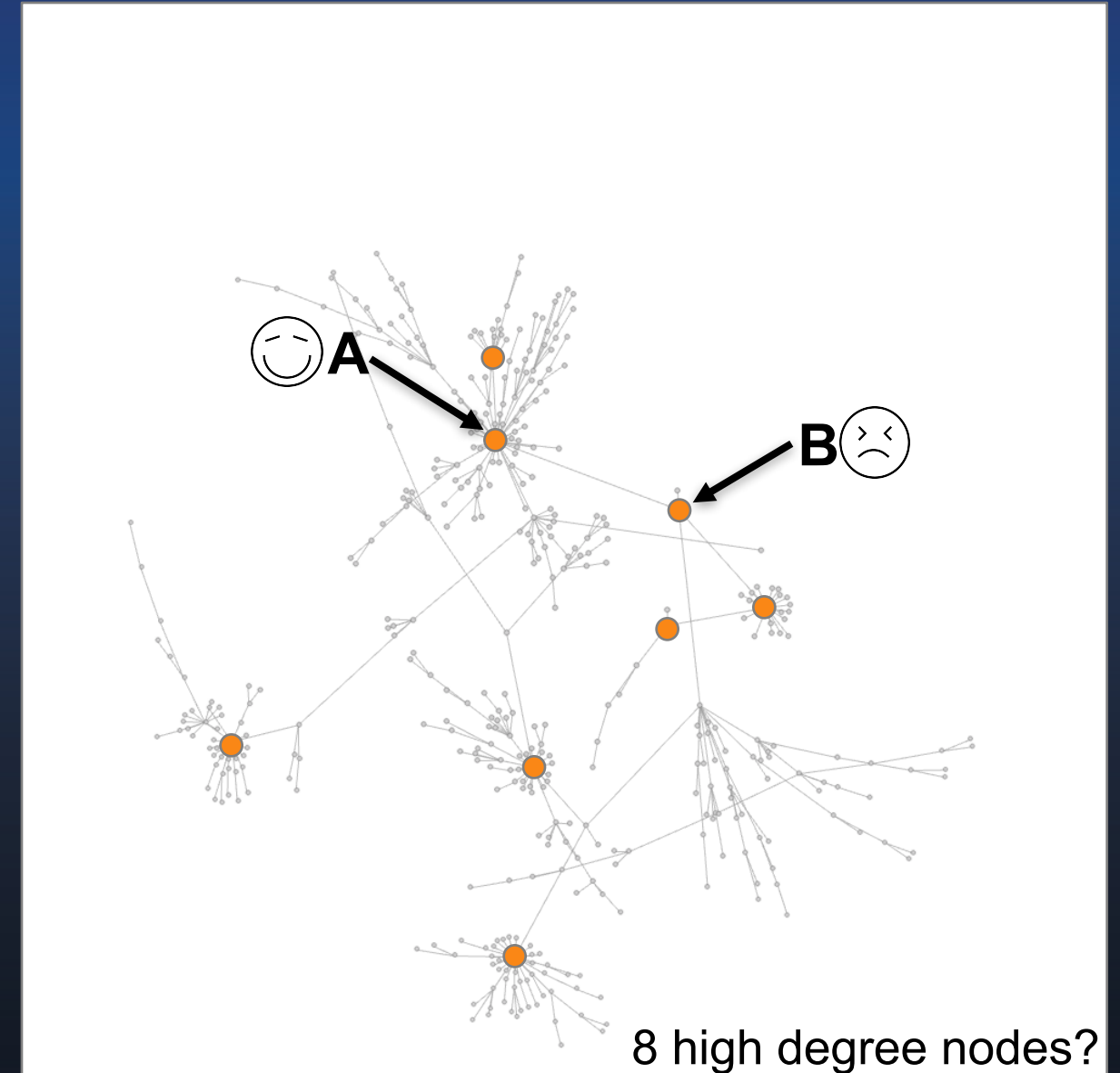
- Selected Sampling Methods
- Pilot Study
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# Formal Study I: High Degree Nodes



Original Graph

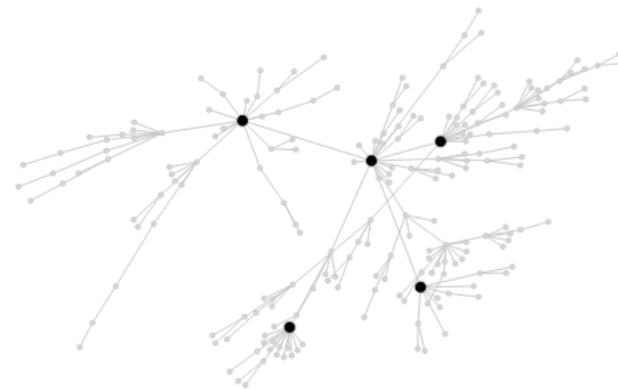


Sampled Graph

# Formal Study I: High Degree Nodes

Graph Sampling Formal Study Experiment I

Sampled Graph:



## Experiment I

Experiment statistics:

Block	1 / 2
Trail	1 / 90

Experiment description:

For the **highlighted nodes** (color in black), please select the ones that you think are **High-Degree Nodes**.

Selected node number: 0

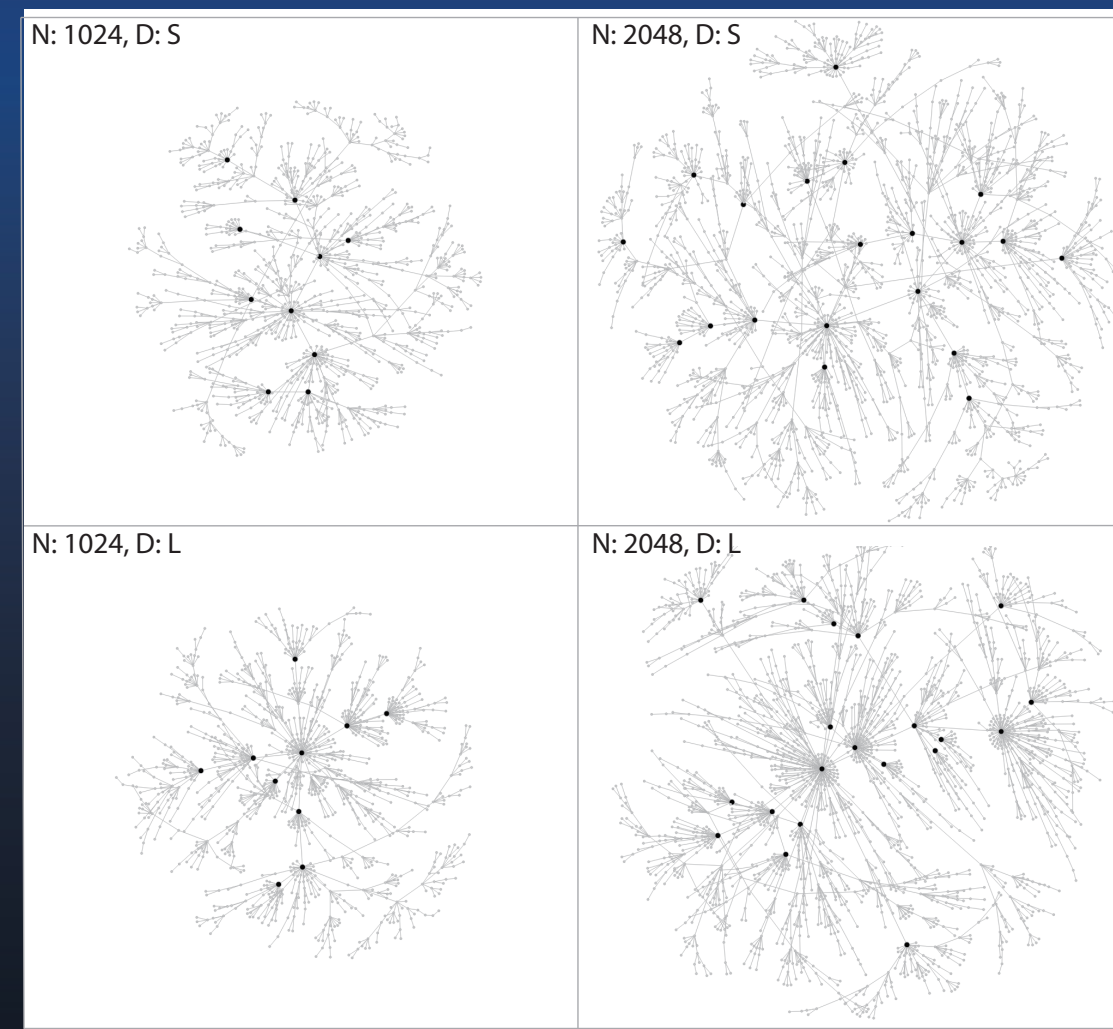
No HDN Nodes

# Formal Study I: High Degree Nodes

	2	graph sizes (small, large)
	2	average degrees of hub nodes (small, large)
	5	sampling strategies ( <i>RN</i> , <i>REN</i> , <i>RW</i> , <i>RJ</i> , <i>FF</i> )
	3	random seeds (3 different seeds)
×	3	repetitions
<hr/>		
	180	trials per participant
×	20	participants
<hr/>		
	<b>3,600</b>	<b>trials in total</b>

## Experiment Setting

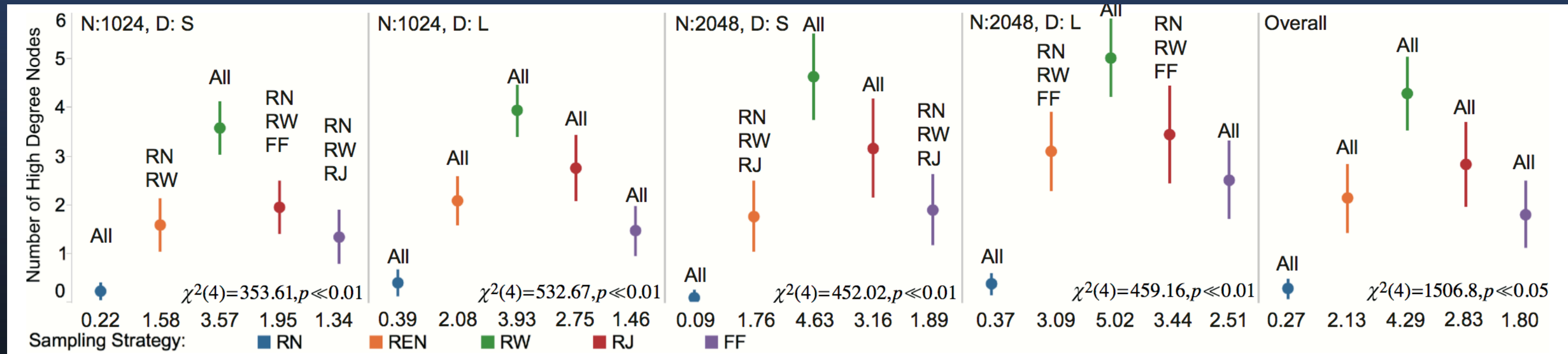
20 high degree nodes



## Data Generation

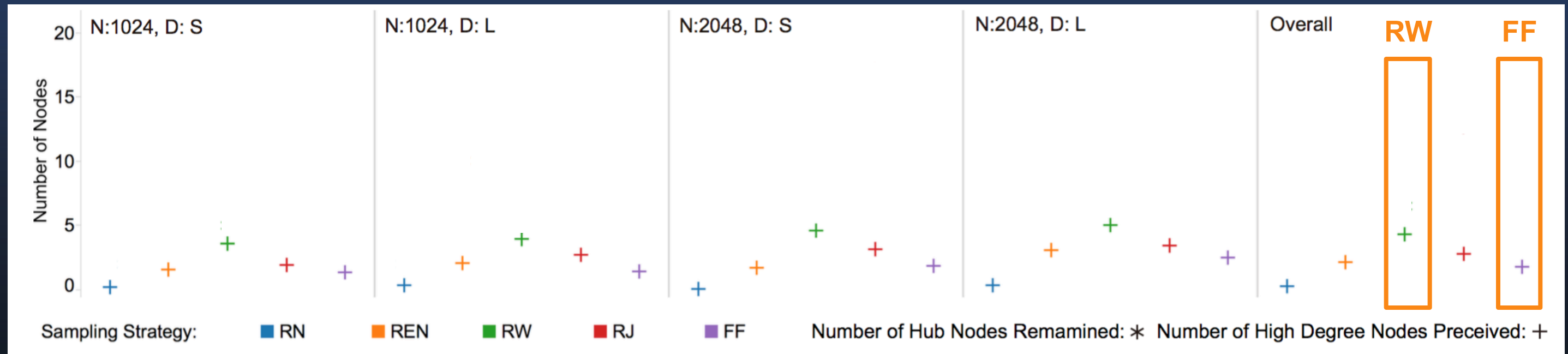
# Formal Study I: High Degree Nodes Results

- Discussions:
  - It is easier to perceive high degree nodes in the *RW* Samples
  - It is more difficult to perceive high degree nodes in *RN* Samples
  - Above results hold across datasets



# Formal Study I: High Degree Nodes Results

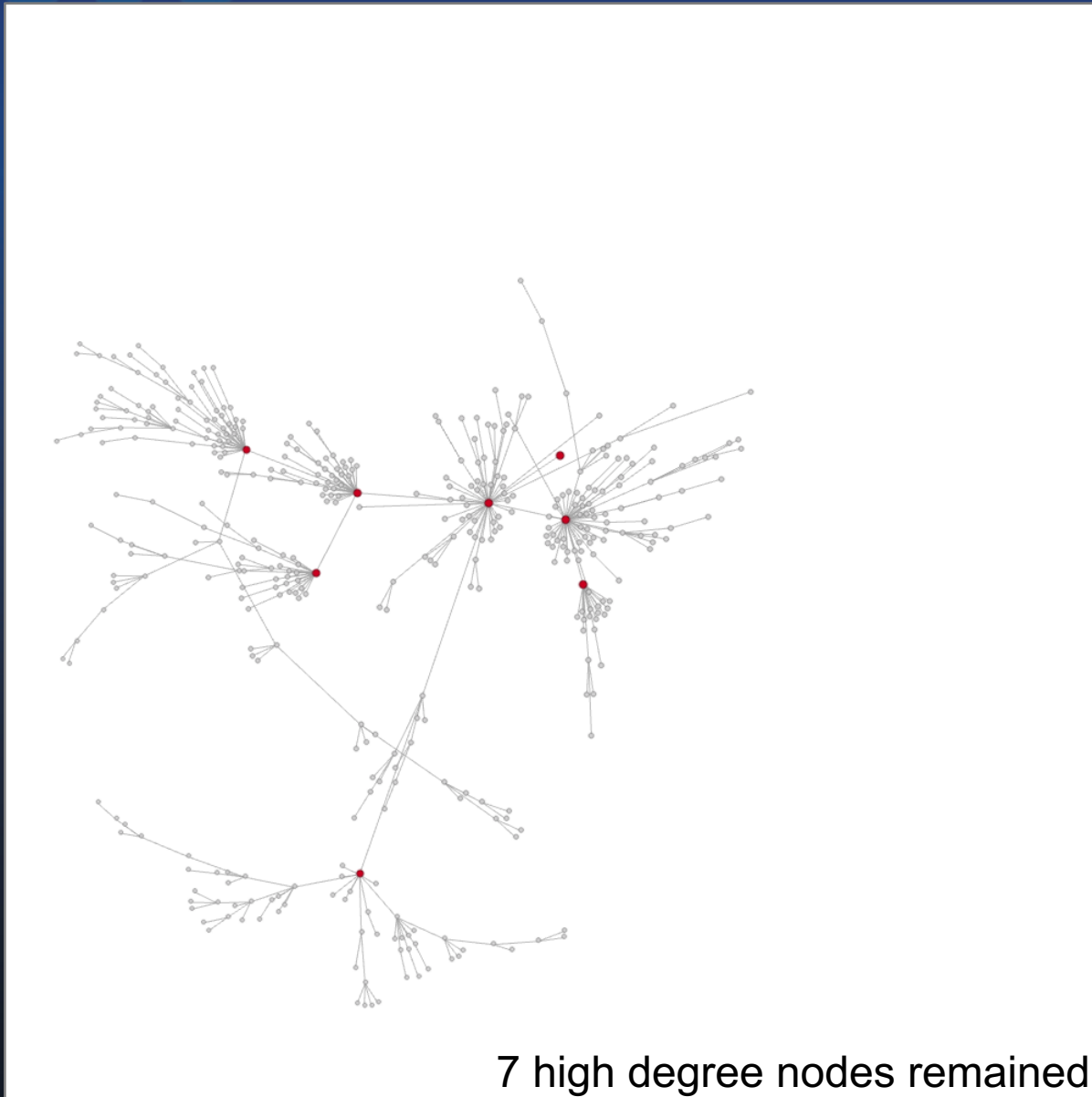
- Discussions:
  - It will be easier to perceive high degree nodes in the *RW* Samples
  - It will be more difficult to perceive high degree nodes in *RN* Samples.
  - Above results hold across datasets



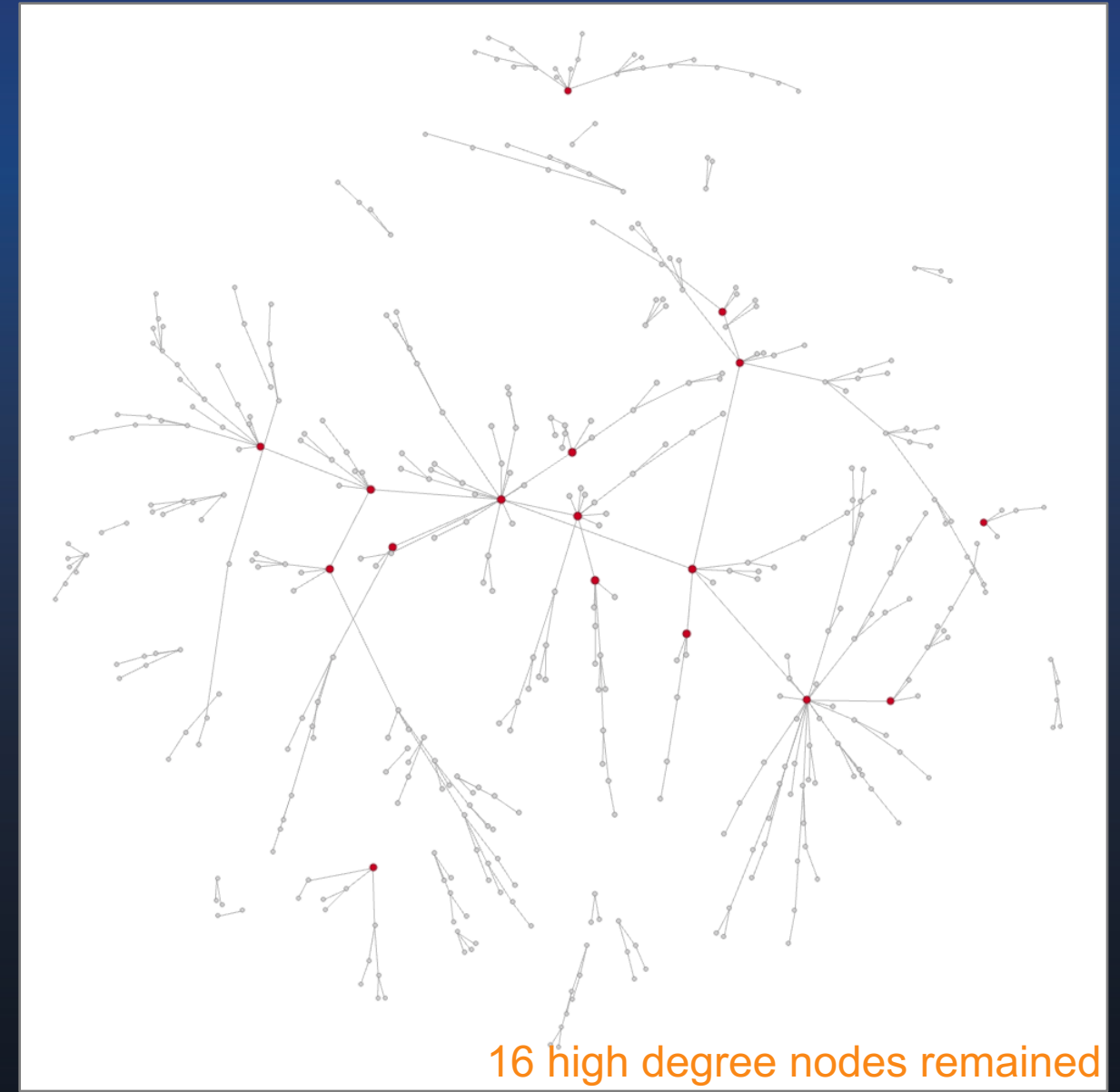
Contradiction with  
metric-based results!

Number of high degree nodes **perceived** (Visualization): +  
Number of high degree nodes **remained** (Data Mining): \*

# Formal Study I: High Degree Nodes Results



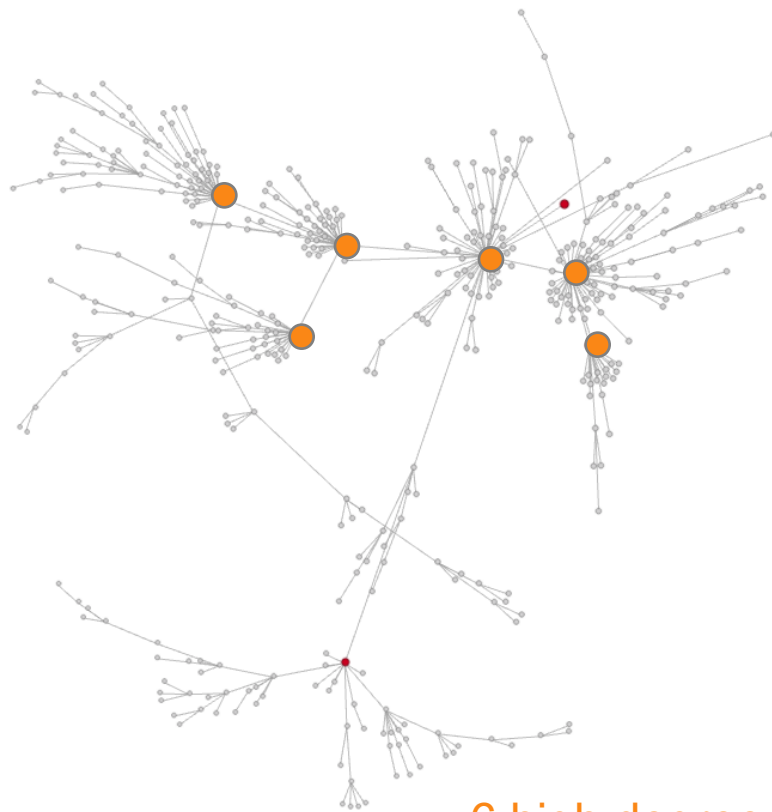
Random Walk (RW)



Forest Fire (FF)

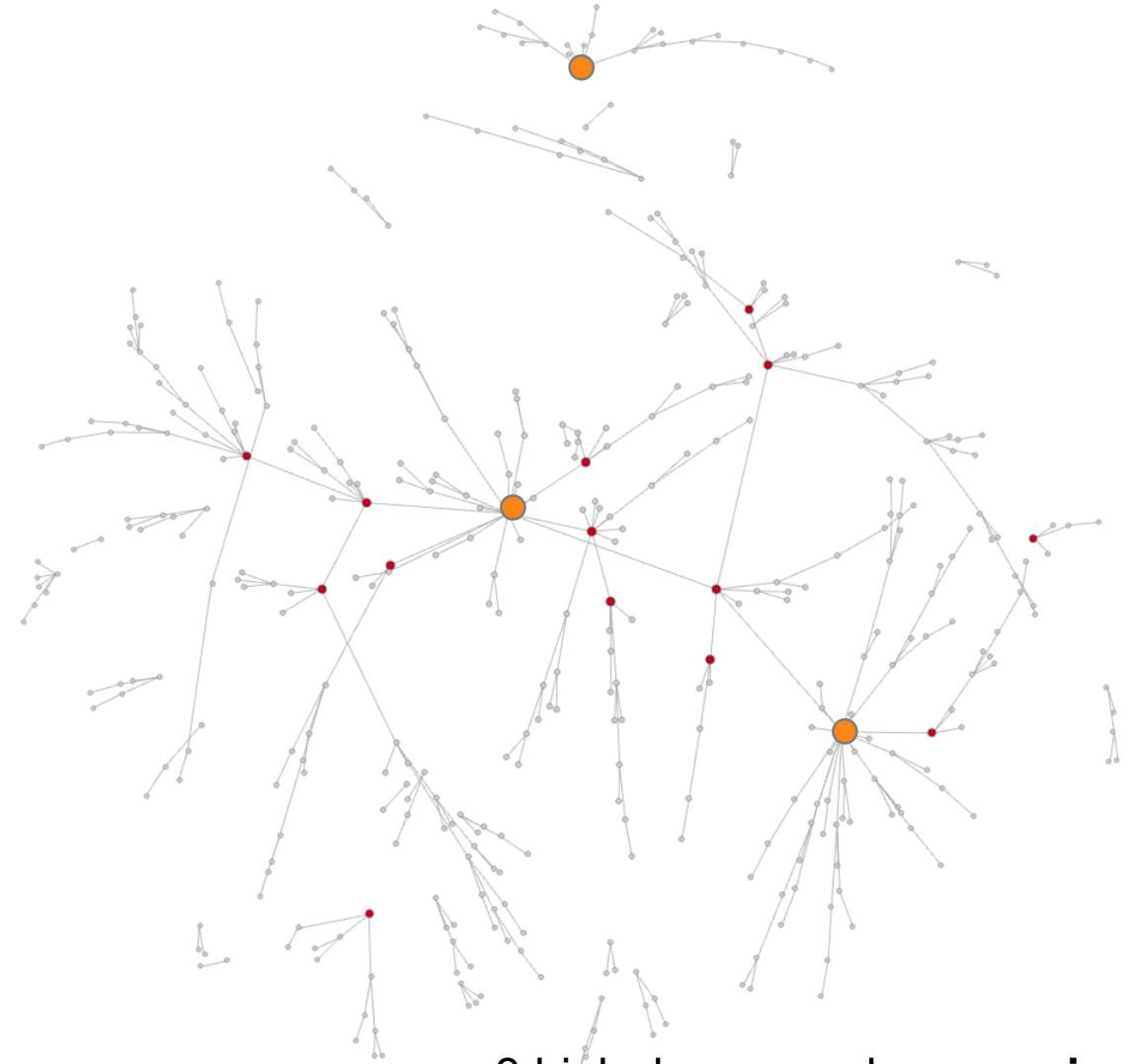


# Formal Study I: High Degree Nodes Results



6 high degree nodes **perceived**  
~~7 high degree nodes remained~~

Random Walk (RW)



3 high degree nodes **perceived**  
16 high degree nodes remained

Forest Fire (FF)



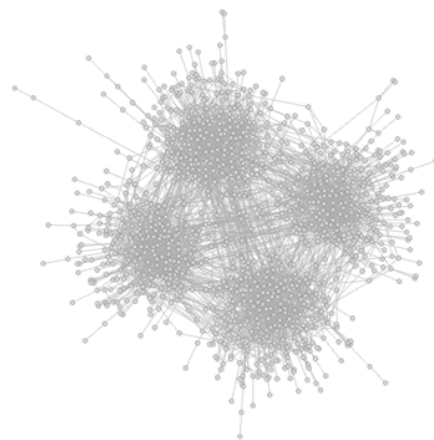
# Outline

- Selected Sampling Methods
- Pilot Study
- Formal Studies
  - Perception of High Degree Nodes (more high degree nodes are perceived in *RW*)
  - Perception of Cluster Quality
  - Perception of Coverage Area

# Formal Study II: Cluster Quality

## Graph Sampling Formal Study Experiment II

Original Graph:



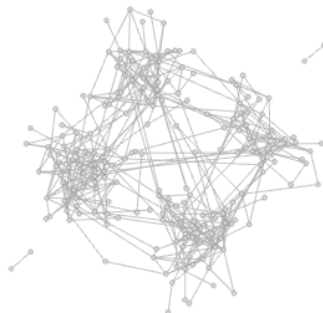
Graph I: ☆☆☆☆



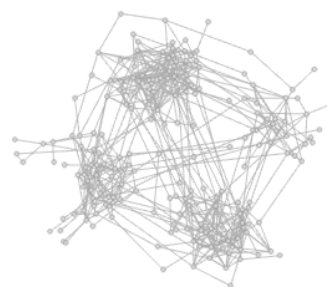
Graph II: ☆☆☆☆



Graph III: ☆☆☆☆



Graph IV: ☆☆☆☆



Graph V: ☆☆☆☆



### Experiment II

#### Experiment statistics:

Block	1 / 2
Trail	1 / 18

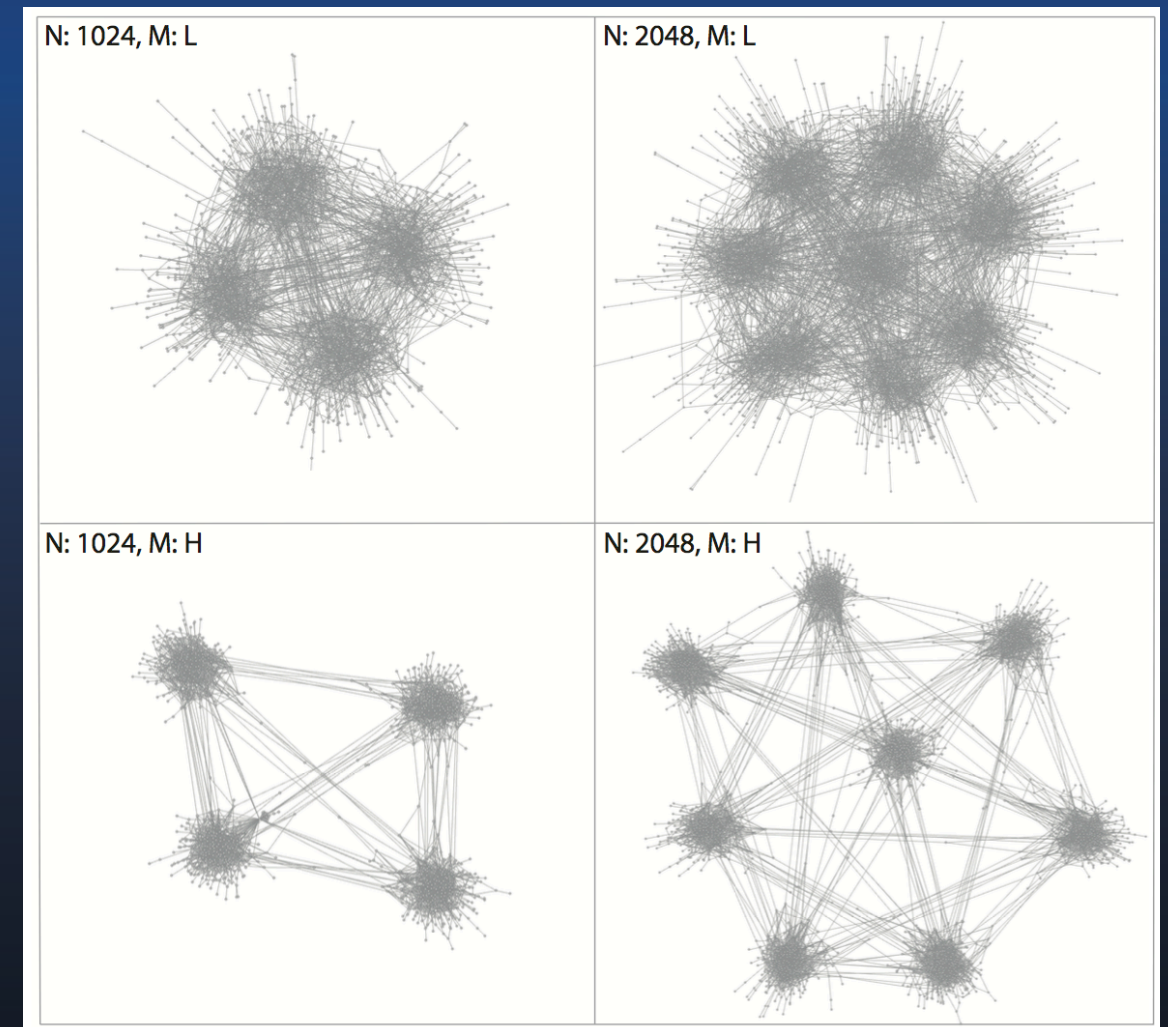
#### Experiment description:

Please rating the **five** sampled graphs based on **Cluster Quality** (1-star is the worst, 5-star is the best).

# Formal Study II: Cluster Quality

	2	graph sizes (small=1024 nodes, large=2048 nodes)
	2	graph modularities (low, high)
	3	random seeds (3 different seeds)
×	3	repetitions
<hr/>		
	36	trials per participant
×	20	participants
<hr/>		
	<b>720</b>	<b>trials in total</b>

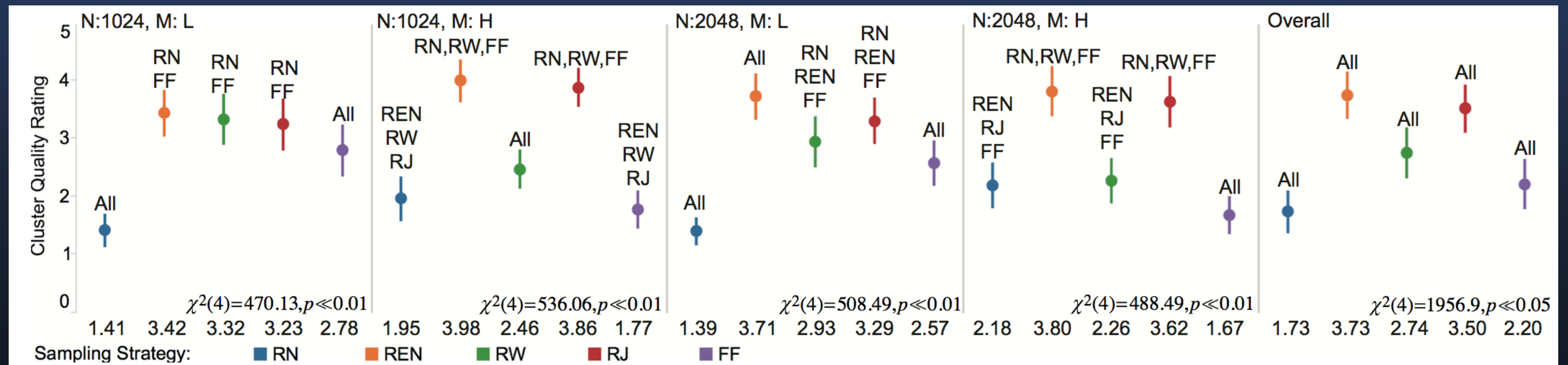
## Experiment Setting



## Data Generation

# Formal Study II: Cluster Quality Results

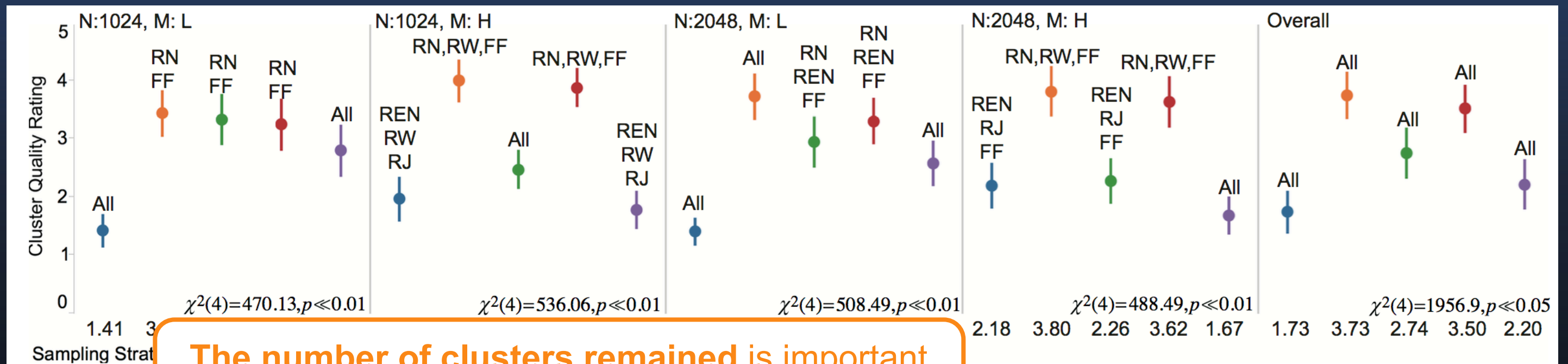
- Discussions:
  - RE* and *RJ* best preserve the perceived cluster quality in samples
  - RN* and *FF* struggles in preserving the perceived cluster quality
  - The performance of *RW* and *FF* depends on graph modularity





# Formal Study II: Cluster Quality Results

Graph	N: 1024, M: L				N: 1024, M: H				N: 2048, M: L				N: 2048, M: H				Overall			
	M	CN	CS	ER	M	CN	CS	ER	M	CN	CS	ER	M	CN	CS	ER	M	CN	CS	ER
Original	0.55	4	256	0.50	0.68	4	256	0.15	0.67	8	256	0.50	0.80	8	256	0.15	0.68	6	256	0.33
RN	0.77	4.6	14.0	0.15	0.80	4.3	15.9	0.07	0.84	2.4	21.7	0.08	0.88	4.1	26.4	0.02	0.82	3.8	19.5	0.08
REN	0.62	6	14.0	0.15	0.72	<b>4.0</b>	50.0	0.03	0.73	<b>8.0</b>	50.2	0.17	0.85	<b>8.0</b>	50.4	0.02	0.73	6.2	48.4	0.10
RW	0.59	<b>4.2</b>	<b>48.2</b>	0.20	0.57	4.4	48.0	<b>0.20</b>	0.70	<b>8.0</b>	51.5	<b>0.19</b>	0.74	6.0	68.2	<b>0.03</b>	<b>0.65</b>	5.6	<b>54.0</b>	0.16
RJ	0.60	4.9	41.5	0.22	<b>0.69</b>	<b>4.0</b>	<b>50.5</b>	0.03	0.72	<b>8.0</b>	51.0	0.16	<b>0.83</b>	<b>8.0</b>	51.0	0.02	<b>0.71</b>	6.2	48.5	0.11
FF	<b>0.56</b>	4.9	41.8	<b>0.27</b>	0.45	6.5	33.5	0.62	<b>0.69</b>	7.5	<b>53.9</b>	0.17	0.66	5.0	<b>80.8</b>	<b>0.03</b>	0.59	<b>6.0</b>	52.5	<b>0.27</b>



The number of clusters remained is important for perceiving the cluster quality in visualization!





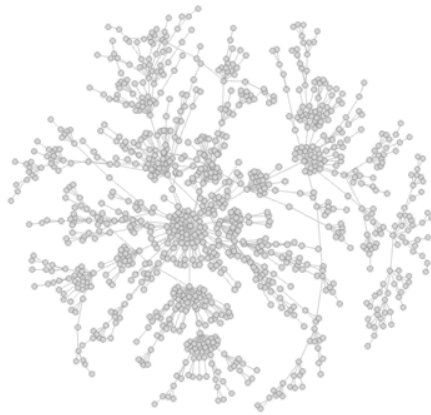
# Outline

- Selected Sampling Methods
- Pilot Study
- Formal Studies
  - Perception of High Degree Nodes (more high degree nodes are perceived in *RW*)
  - Perception of Cluster Quality (cluster number is important)
  - Perception of Coverage Area

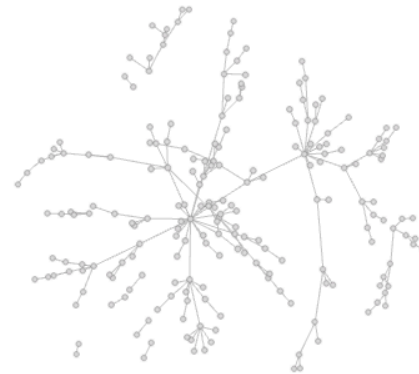
# Formal Study III: Coverage Area

## Graph Sampling Formal Study Experiment III

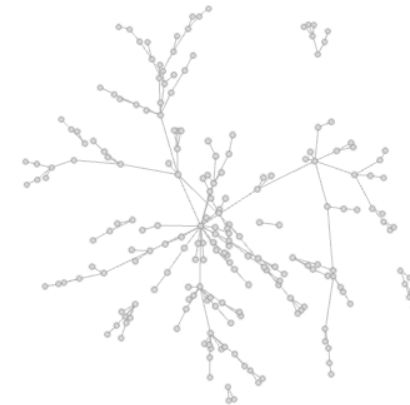
Original Graph:



Graph I: ☆☆☆☆☆



Graph II: ☆☆☆☆☆



Graph III: ☆☆☆☆☆



Graph IV: ☆☆☆☆☆



Graph V: ☆☆☆☆☆



### Experiment III

#### Experiment statistics:

Block	1 / 4
Trail	1 / 18

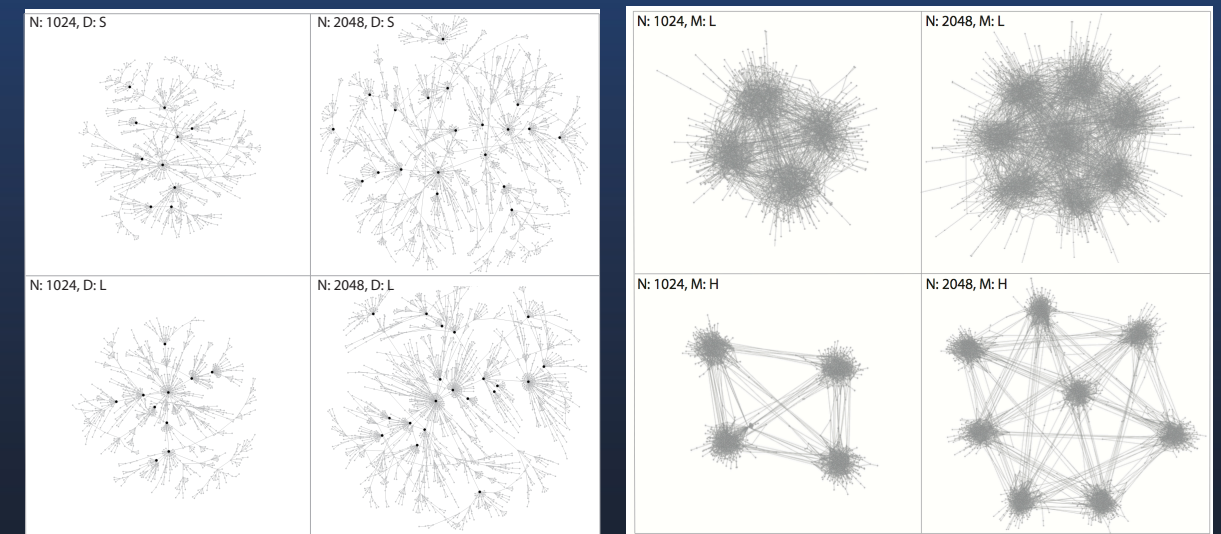
#### Experiment description:

Please rating the **five** sampled graphs based on **Coverage Area** (1-star is the worst, 5-star is the best).

# Formal Study III: Coverage Area

×	2	graph models (Barabási-Albert model [7] and Sah et al.'s model [46])
	2	graph sizes (small=1024 nodes, large=2048 nodes)
	2	corresponding parameters for each graph model
	3	random seeds (3 different seeds)
	3	repetitions
×	72	trials per participant
	24	participants
1728		trials in total

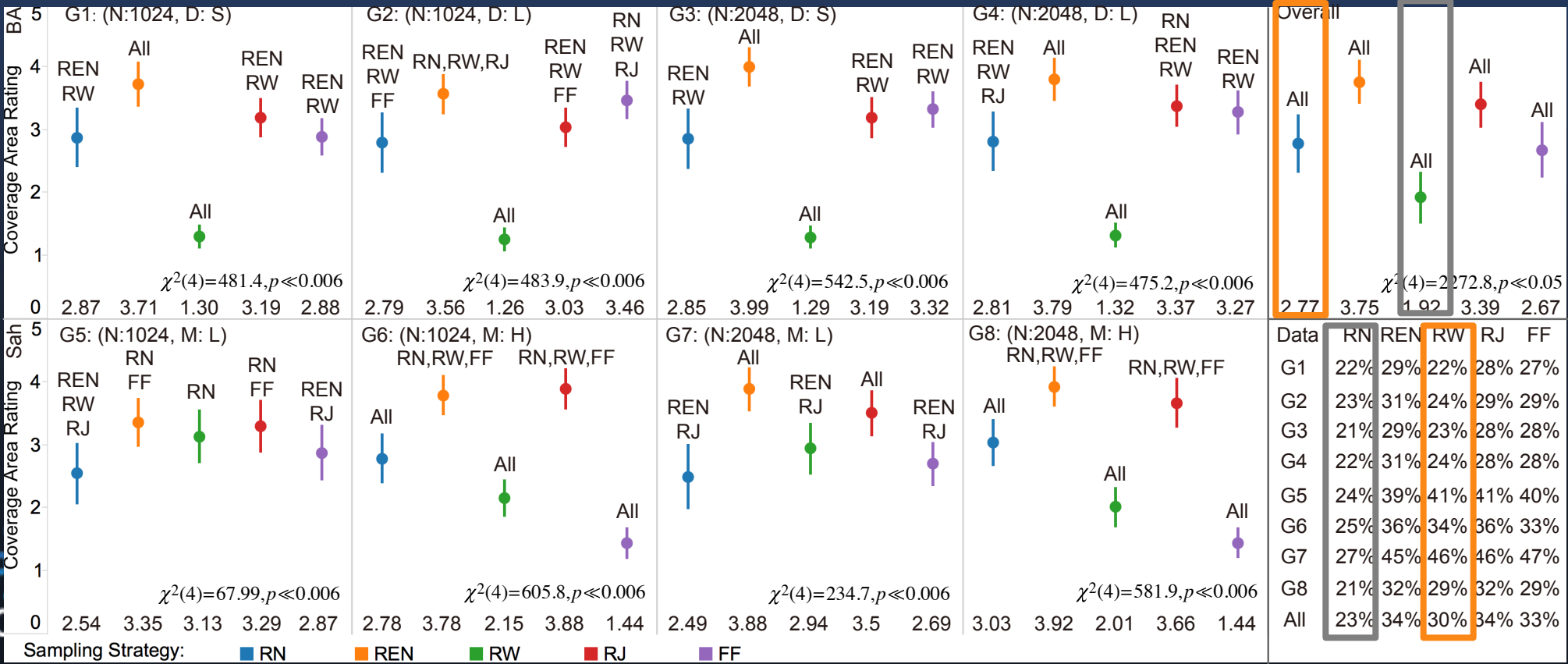
Experiment Setting



Data Generation

# Formal Study III: Coverage Area Results

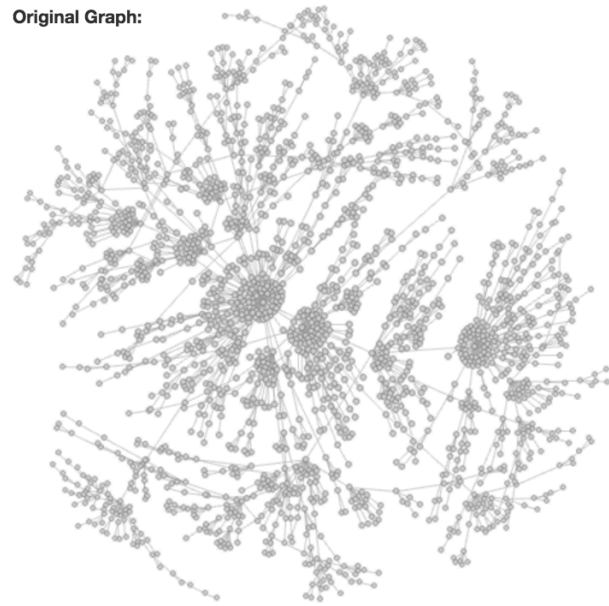
- Discussions:
  - RE* and *RJ* have the largest perceived coverage area
  - RW* has a smallest perceived coverage area in most cases
  - RW* and *FF* 's performance vary depending on graph properties



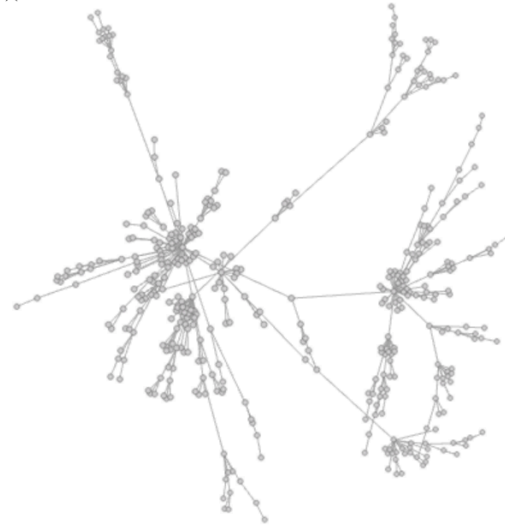
Contradiction with metric-based results!

# Formal Study III: Coverage Area Results

Original Graph:

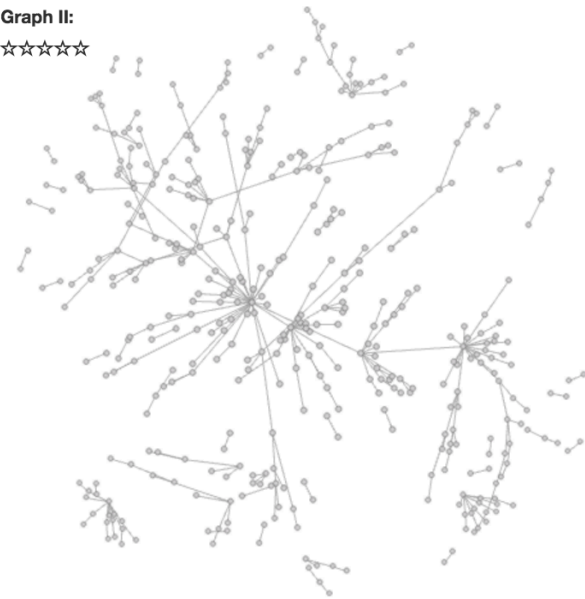


Graph I:  
☆☆☆☆☆

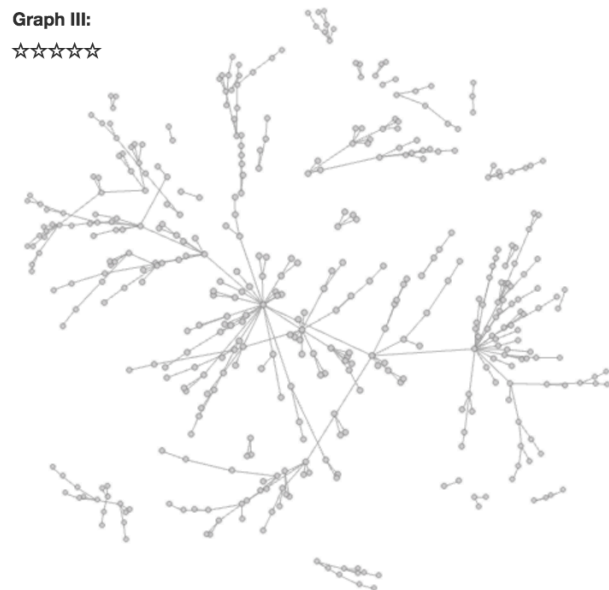


RW

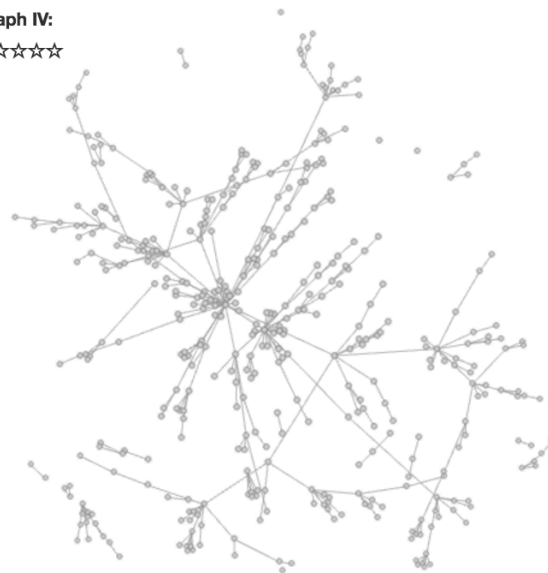
Graph II:  
☆☆☆☆☆



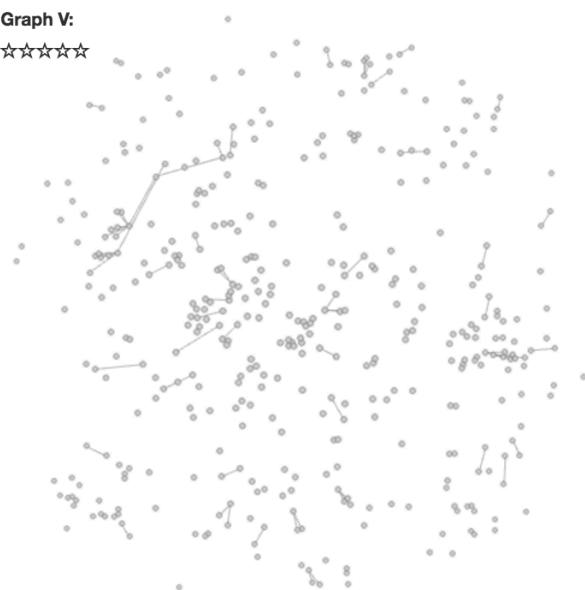
Graph III:  
☆☆☆☆☆



Graph IV:  
☆☆☆☆☆



Graph V:  
☆☆☆☆☆



RN

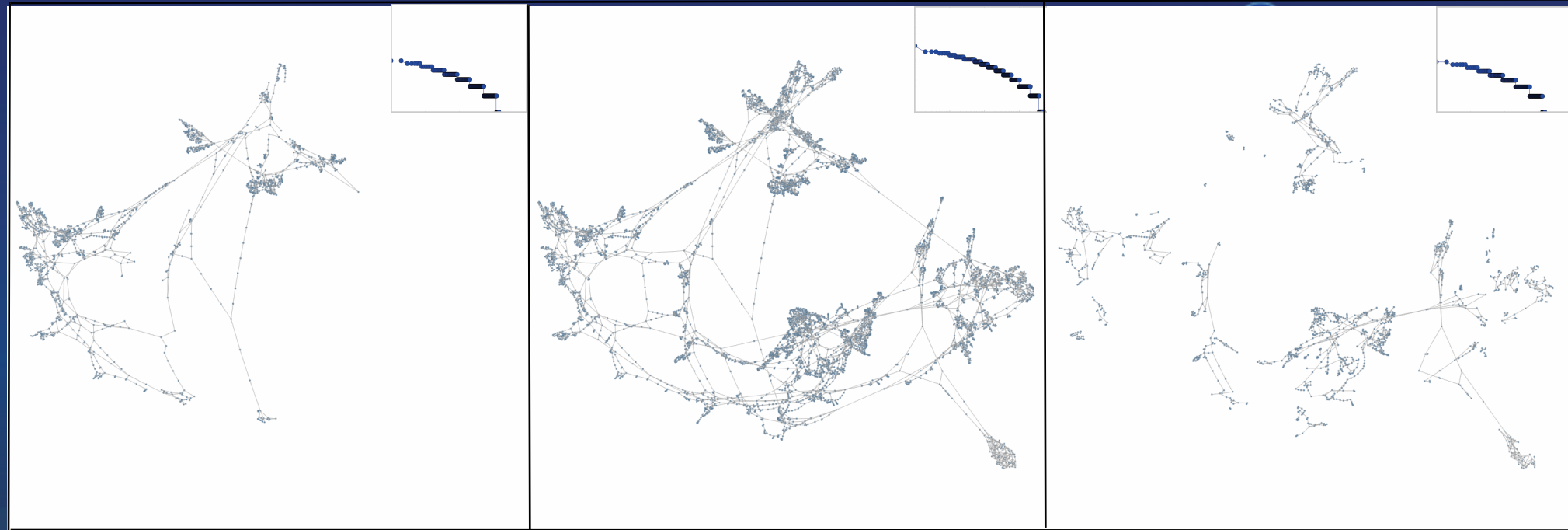
# Conclusion

- We provided the first study of how **graph sampling strategies** can influence the **perception** of node-link visualizations
  - Important visual factors: high degree nodes, cluster quality, and coverage area
  - Recommendations for sampling network visualizations:
    - Recommend **Random Edge** and **Random Jump** for global structure and cluster quality
    - Recommend **Random Walk** for perceived high degree nodes
    - Use **Random Node** unless for specific requirements
    - **Random Walk** and **Forest Fire** are modularity sensitive

Graph sampling performance in visualization may **VARY** from previous metric-based results!



# Q&A



## Evaluation of Graph Sampling: A Visualization Approach

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